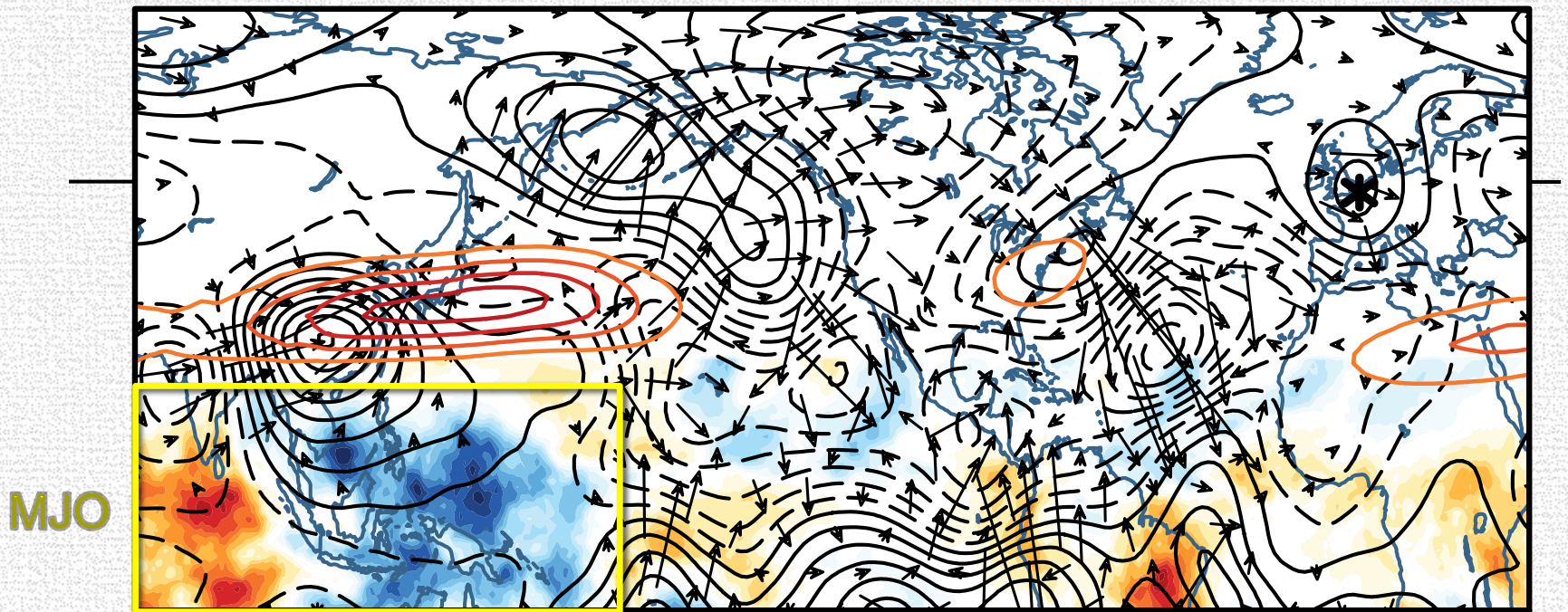
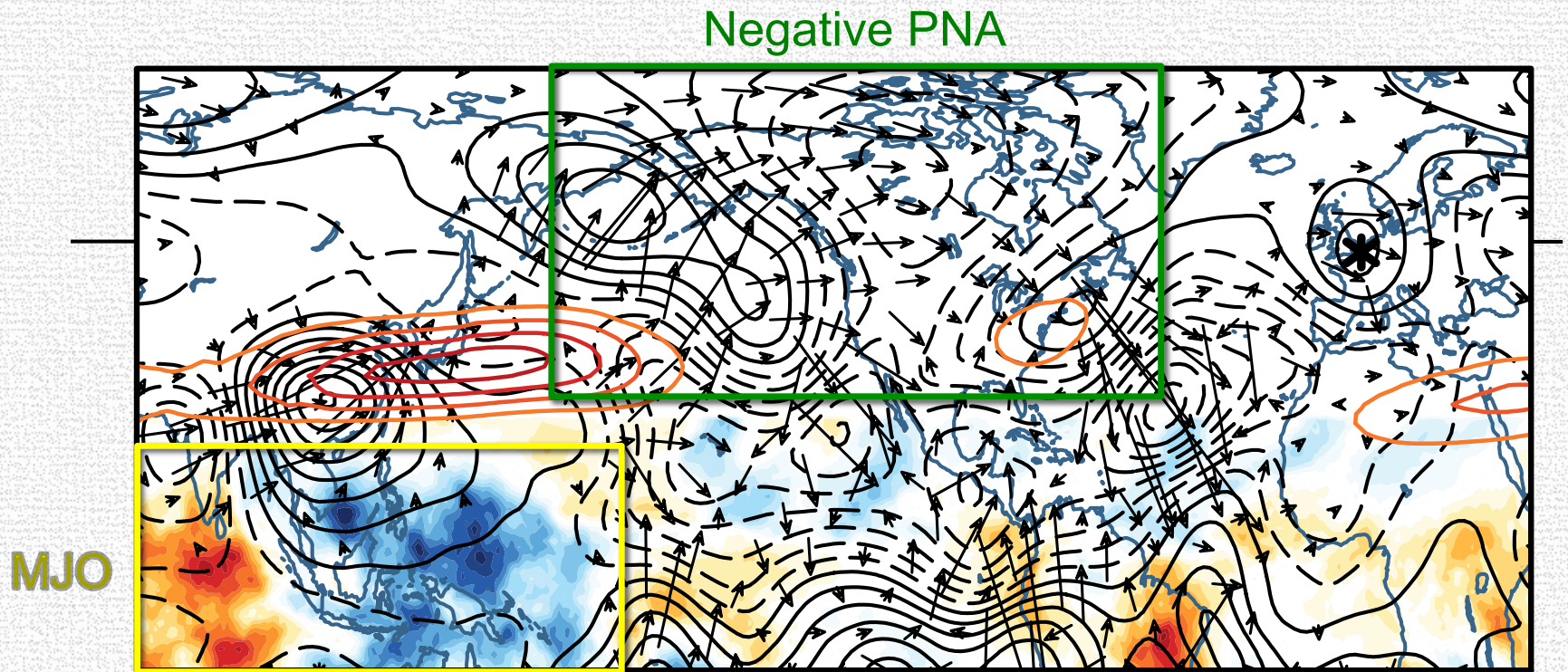


# THE ROLE OF TROPICAL-EXTRATROPICAL INTERACTIONS ON THE OPTIMAL GROWTH OF MADDEN-JULIAN OSCILLATION EVENTS



**Stephanie A. Henderson**  
Daniel J. Vimont  
Matthew Newman

# THE ROLE OF TROPICAL-EXTRATROPICAL INTERACTIONS ON THE OPTIMAL GROWTH OF THE PACIFIC-NORTH AMERICAN PATTERN



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# Data

- ERA-Interim reanalysis:
  - 200-hPa and 850-hPa streamfunction (15°N – 90°N)
  - Vertically integrated apparent heat source (Q1; Yanai et al. 1973) 20°S – 15°N
- NOAA Optimum Interpolation Sea Surface Temperature (OISST) dataset (20°S – 15°N)
- Pentad (5-day) anomalies
- December – February (DJF)
- Range: December 1982 – February 2015
- Daily NOAA/NCEP Climate Prediction Center (CPC) PNA index

# Linear Inverse Modeling (LIM)

$$dx/dt = \mathbf{L}x + \zeta$$

↑  
State of  
system

↑  
Dynamics

↑  
Noise

$$\mathbf{x}(t) = \begin{bmatrix} \text{SST} \\ \text{Q1} \\ \Psi_{200} \\ \Psi_{850} \end{bmatrix}$$

LIM approximates the evolution of a dynamical system by a multivariate linear model

# Linear Inverse Modeling (LIM)

$$dx/dt = \mathbf{L}x + \zeta$$

State of system      Dynamics      Noise

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- The forecast,  $\mathbf{x}(\tau)$ , is the solution to the homogeneous part:

$$\mathbf{x}(\tau) = e^{\mathbf{L}\tau} \mathbf{x}(0)$$

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↑  
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↑  
Dynamics

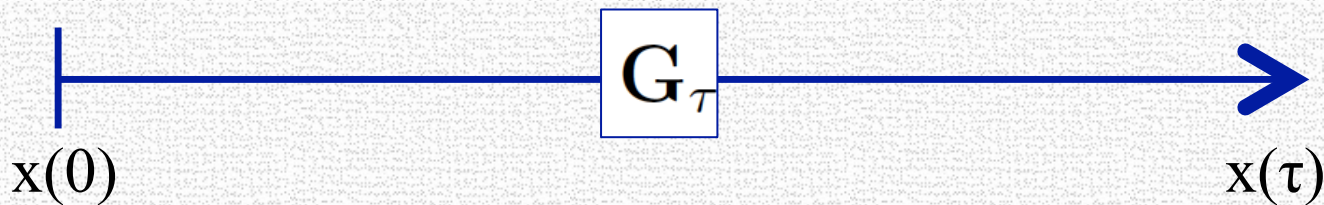
↑  
Noise

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$$\mathbf{x}(\tau) = e^{\mathbf{L}\tau} \mathbf{x}(0) = \mathbf{G}_\tau \mathbf{x}(0)$$

↑  
 $\mathbf{G}_\tau = C_\tau / C_0$





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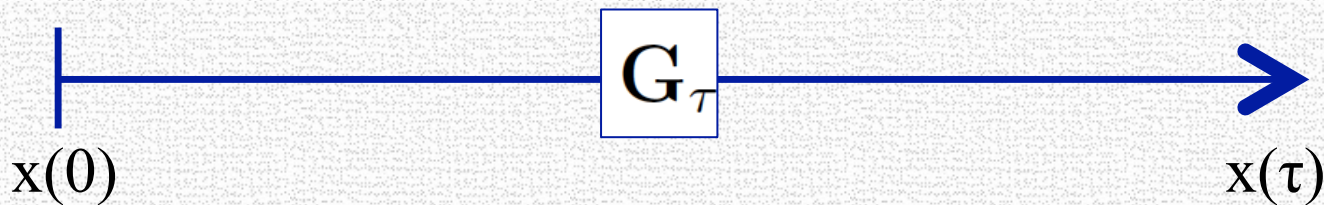
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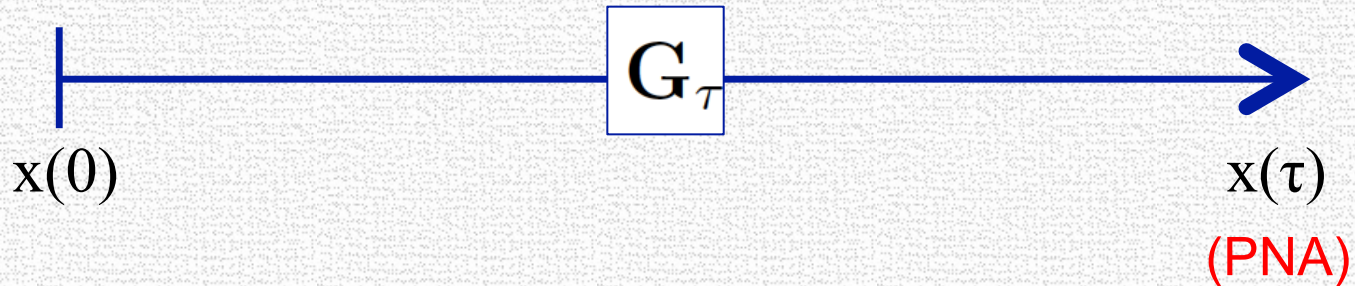
$$\mathbf{x}(\tau) = e^{\mathbf{L}\tau} \mathbf{x}(0) = \mathbf{G}_\tau \mathbf{x}(0)$$

$$\mathbf{L} = \ln(\mathbf{G}_\tau) / \tau$$

$$\mathbf{G}_\tau = C_\tau / C_0$$



# Growth towards the MJO



- We can estimate an optimal initial condition ( $\mathbf{p}$ ) by maximizing growth in the direction of a chosen norm ( $\mathbf{N}$ ) by solving the eigenvalue problem:

$$G_\tau^T \mathbf{N} G_\tau \mathbf{p} - \mu(\tau) \mathbf{p} = 0$$

norm  
(PNA)

eigenvector

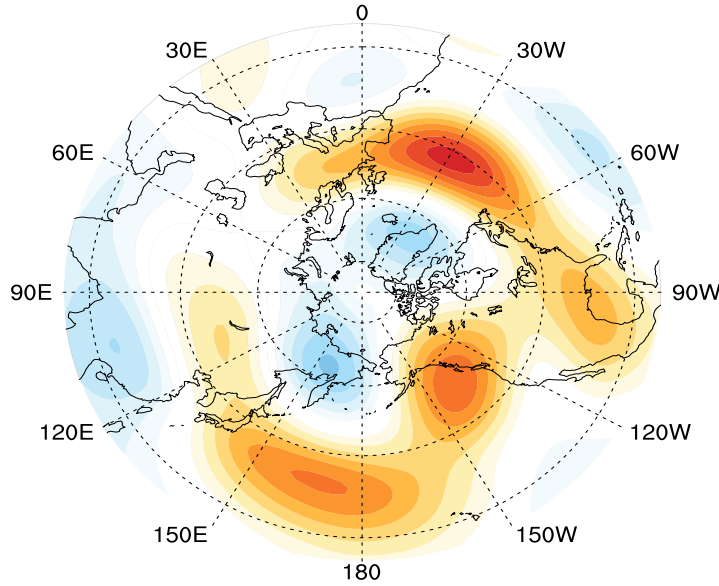
growth



200-hPa  
streamfunction

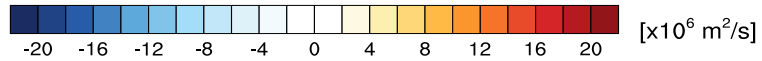
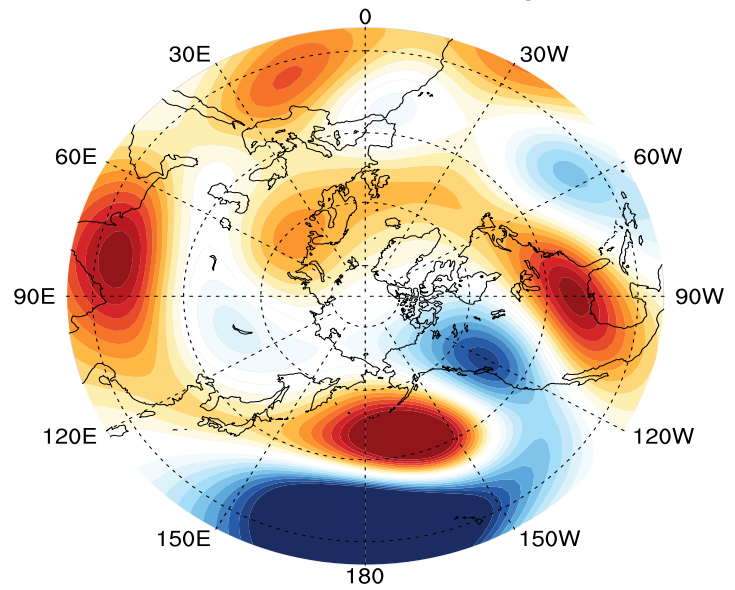
## Initial condition

200mb PSI initial conditions



## Final PNA pattern

200mb PSI final conditions at lag 15

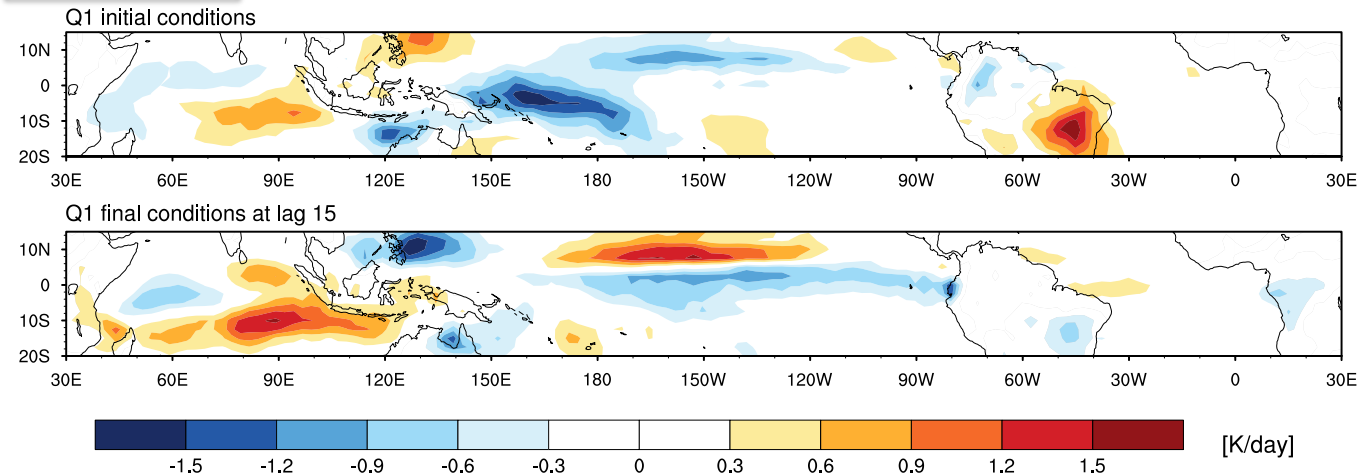
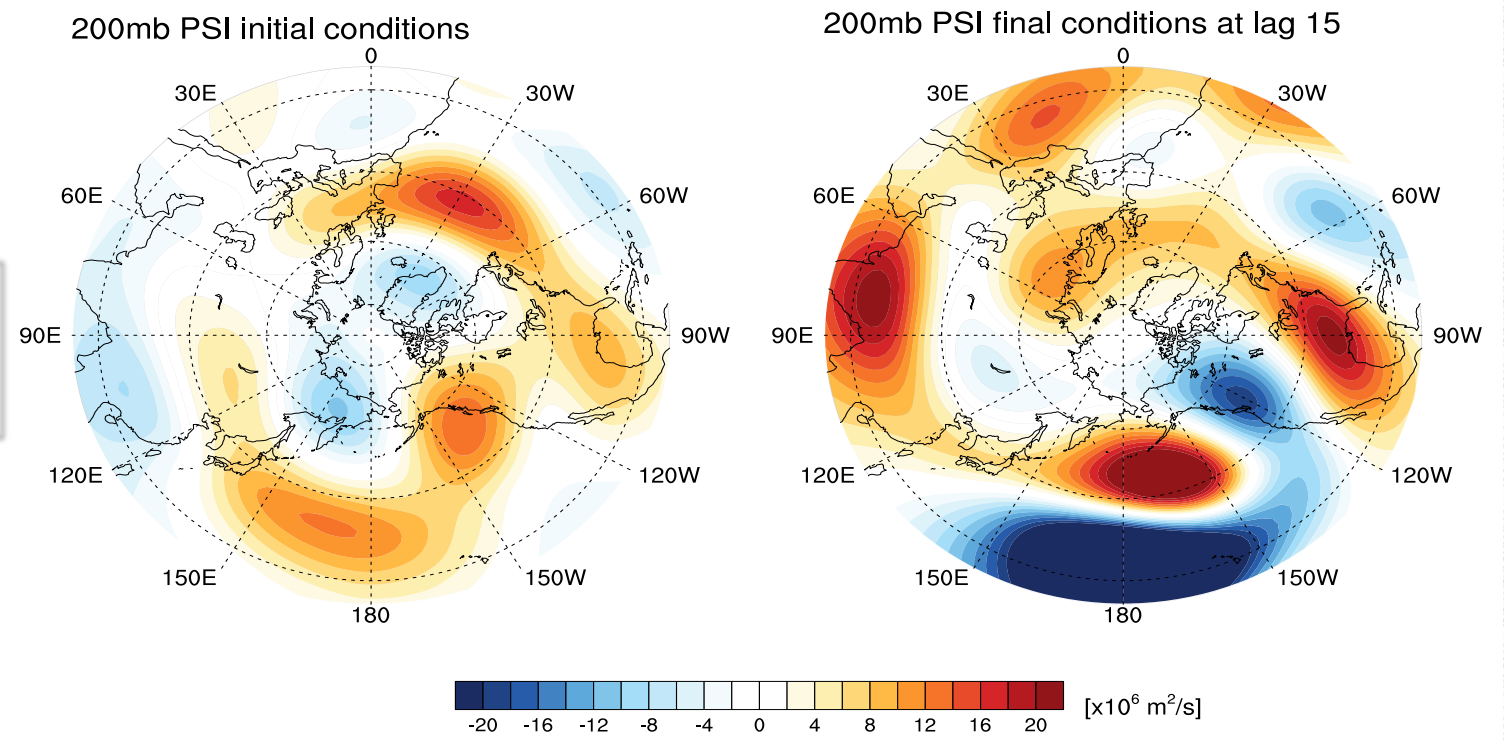


200-hPa  
streamfunction

Q1

Initial condition

Final PNA pattern



Initial condition

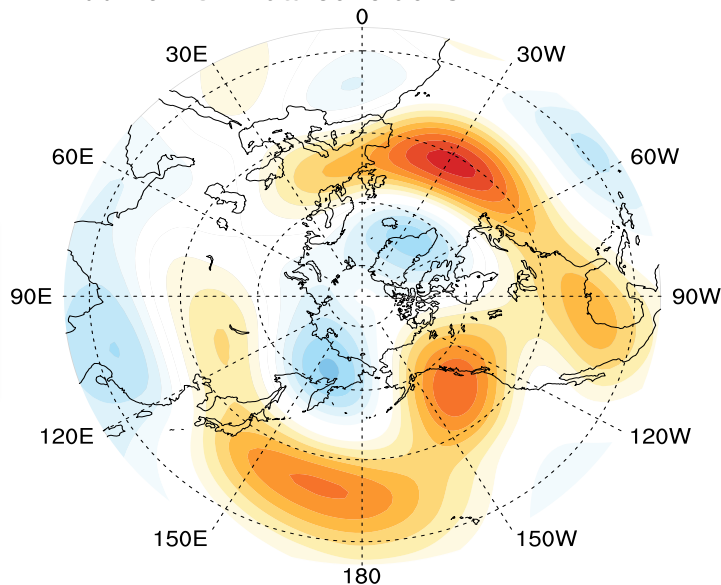
Final condition

## Initial condition

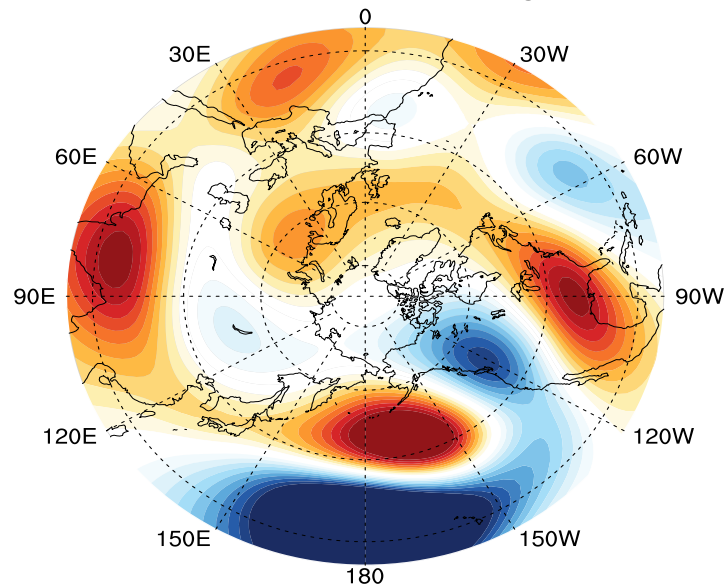
## Final PNA pattern

200-hPa  
streamfunction

200mb PSI initial conditions

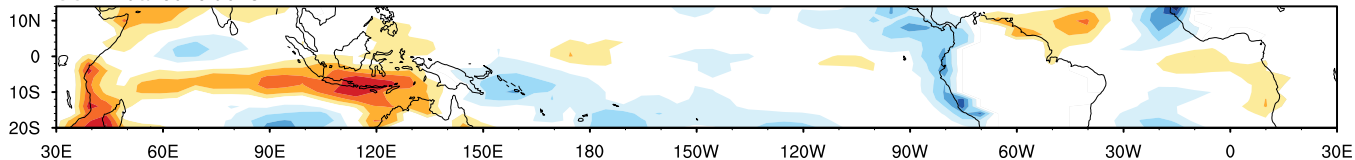


200mb PSI final conditions at lag 15

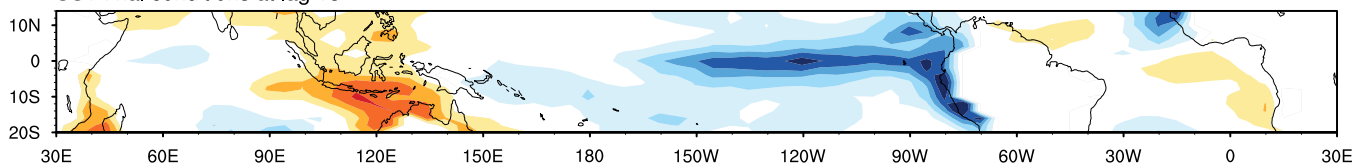


SST

SST initial conditions



SST final conditions at lag 15



Initial condition

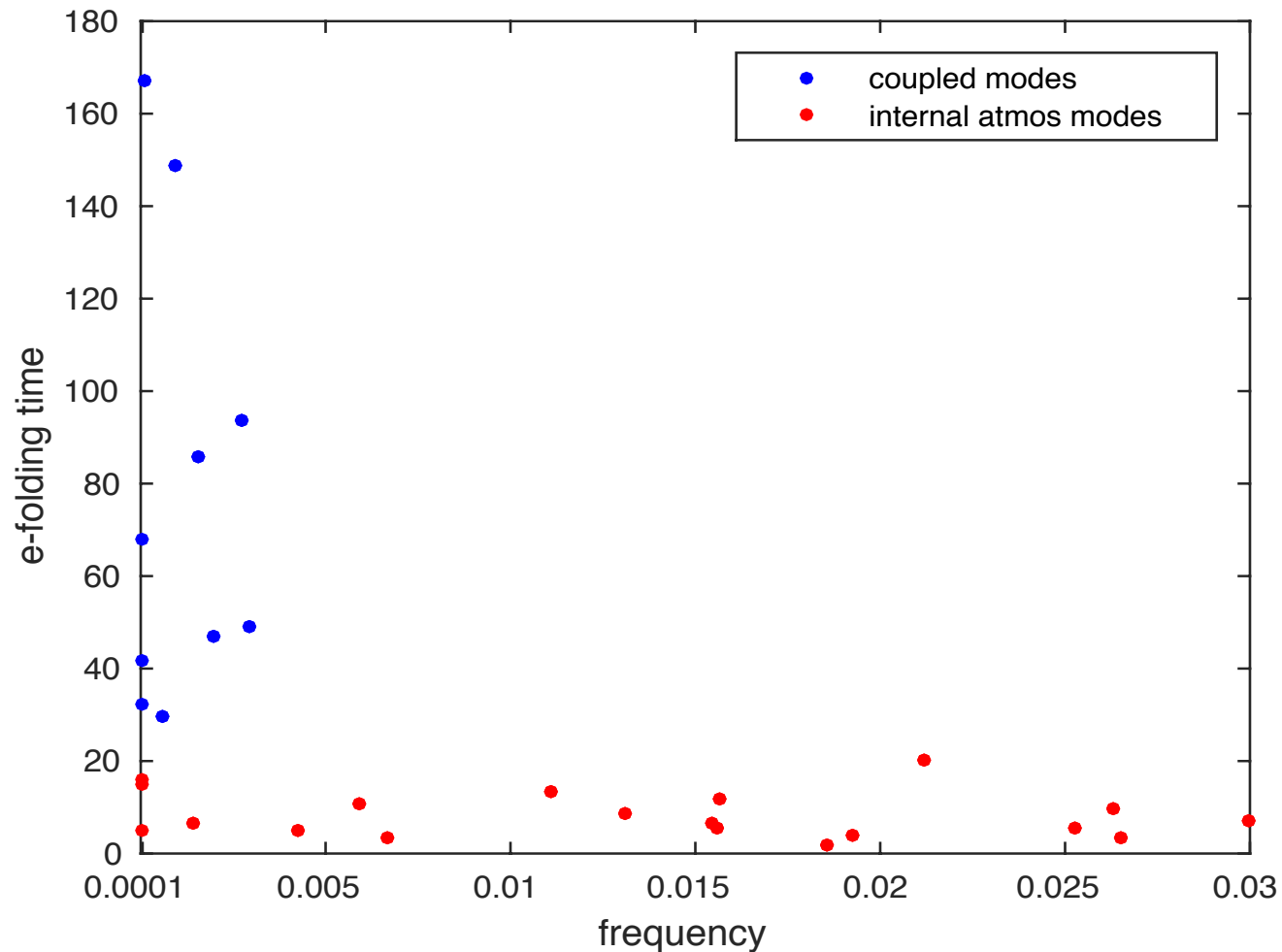
Final condition



# Two eigenspaces of $L$

Recall:  $L = \ln(G_\tau)/\tau$

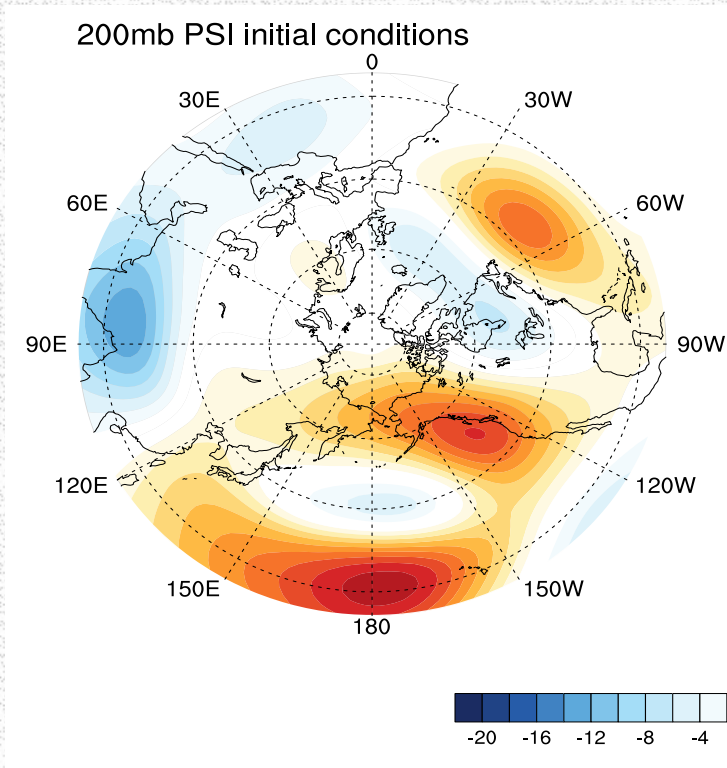
$$G_\tau = C_\tau / C_0$$



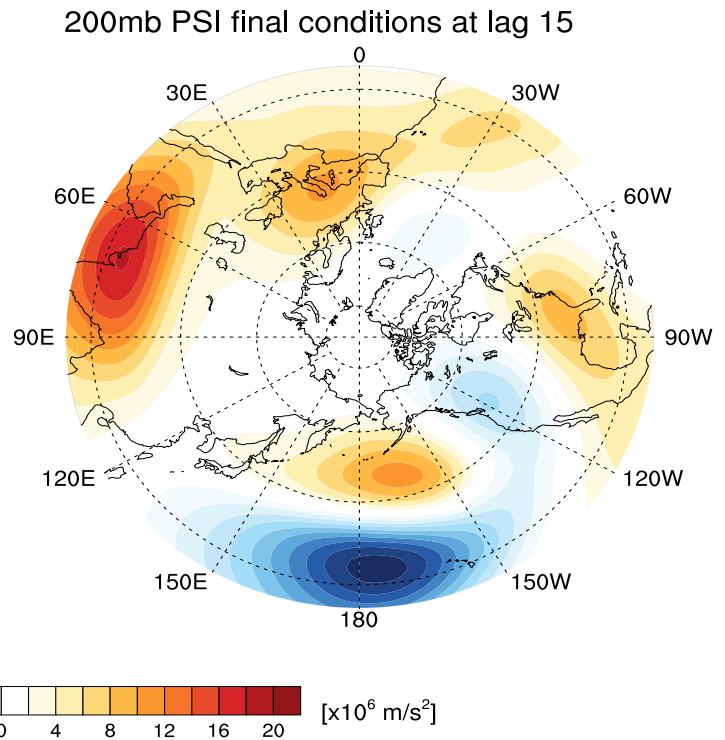
$$\mathbf{G}_\tau = C_\tau / C_0$$


200-hPa  
streamfunction

## Initial Condition



## Final PNA pattern



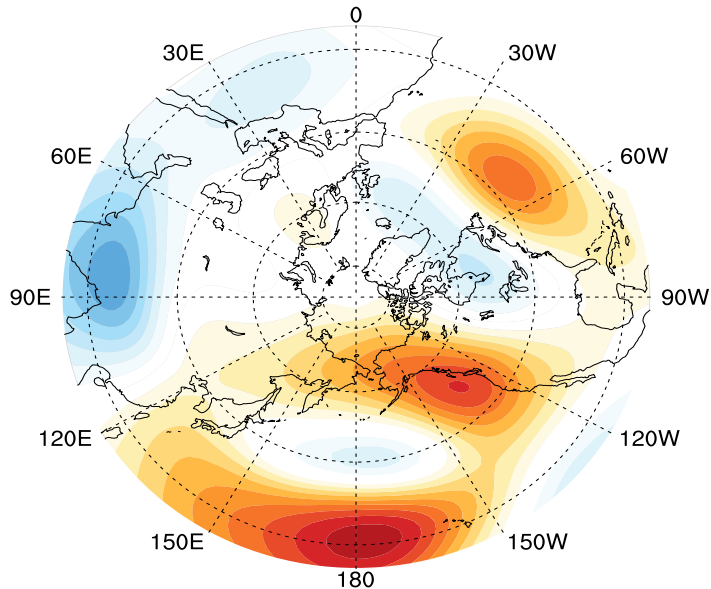


200-hPa  
streamfunction

Q1

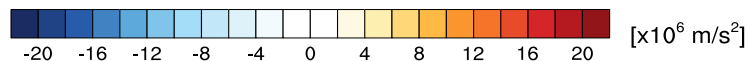
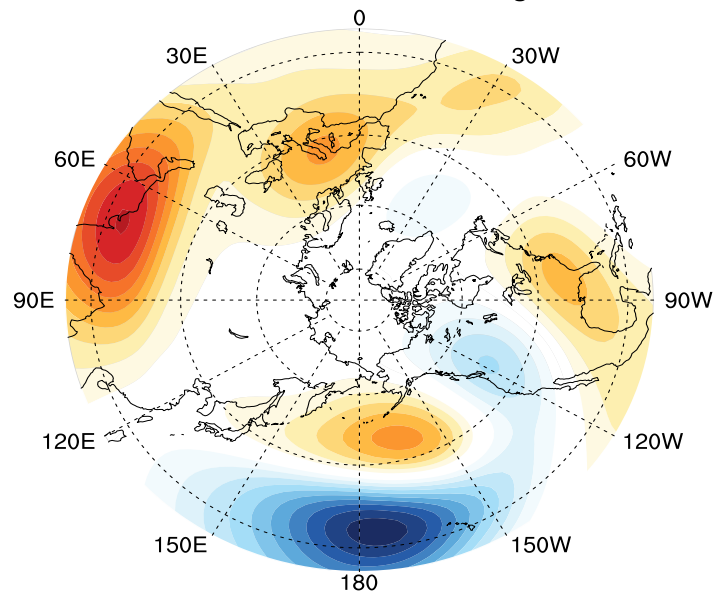
Initial condition

200mb PSI initial conditions

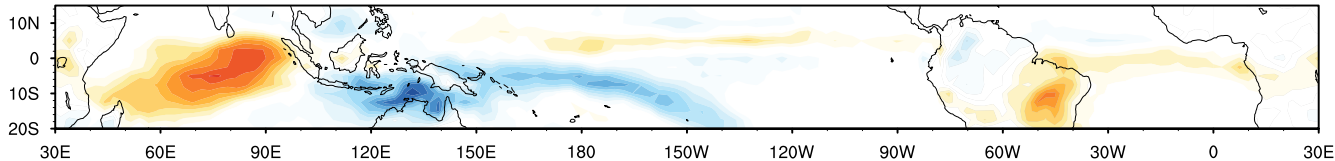


Final PNA pattern

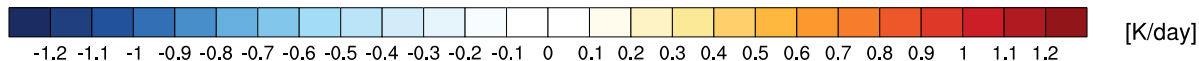
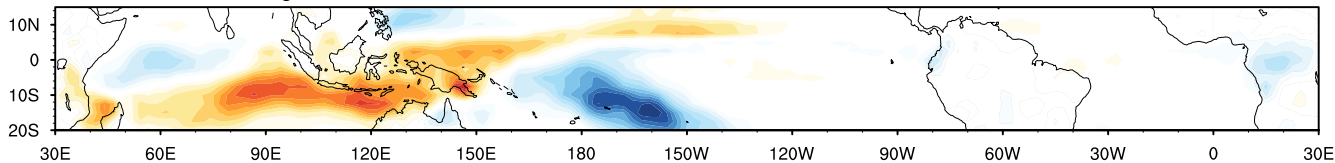
200mb PSI final conditions at lag 15



Q1 initial conditions



Q1 final conditions at lag 15



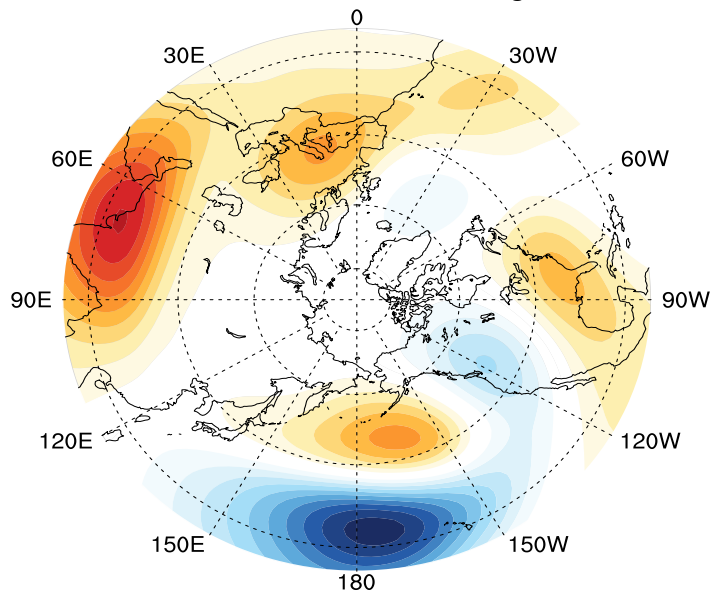
Initial condition

Final condition

# Tropical initial conditions removed

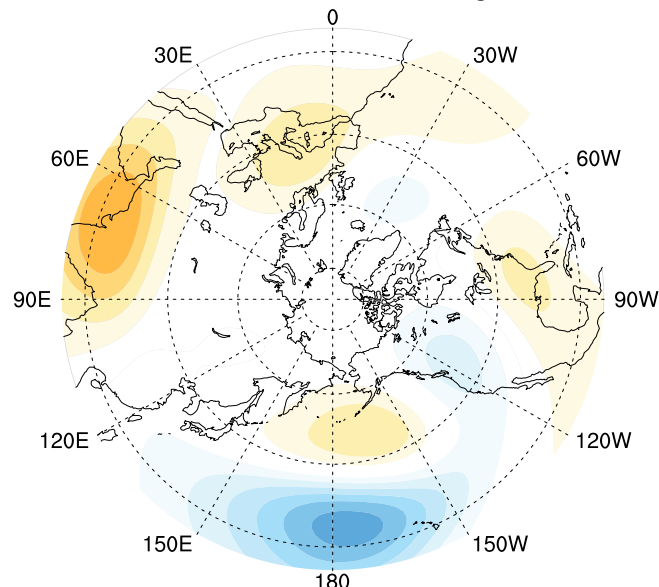
## Unmodified p final PNA

200mb PSI final conditions at lag 15



## Modified p final PNA

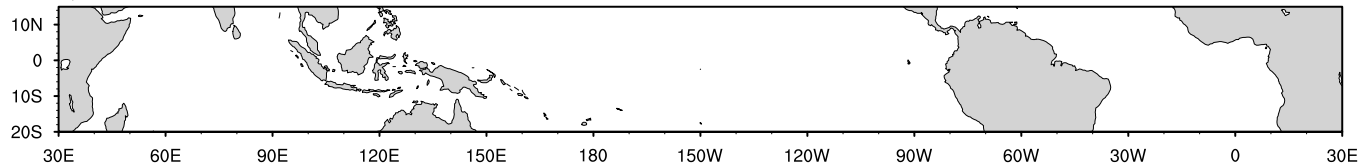
200mb PSI final conditions at lag 15



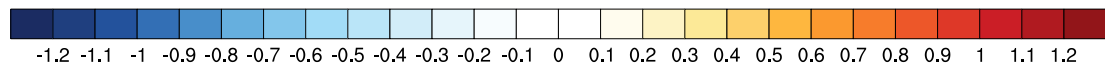
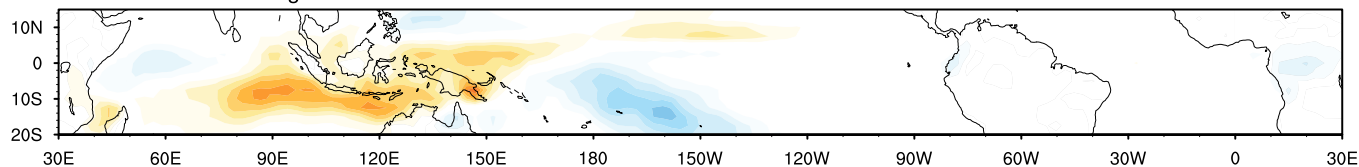
200-hPa  
streamfunction

Q1

Q1 initial conditions



Q1 final conditions at lag 15



[K/day]

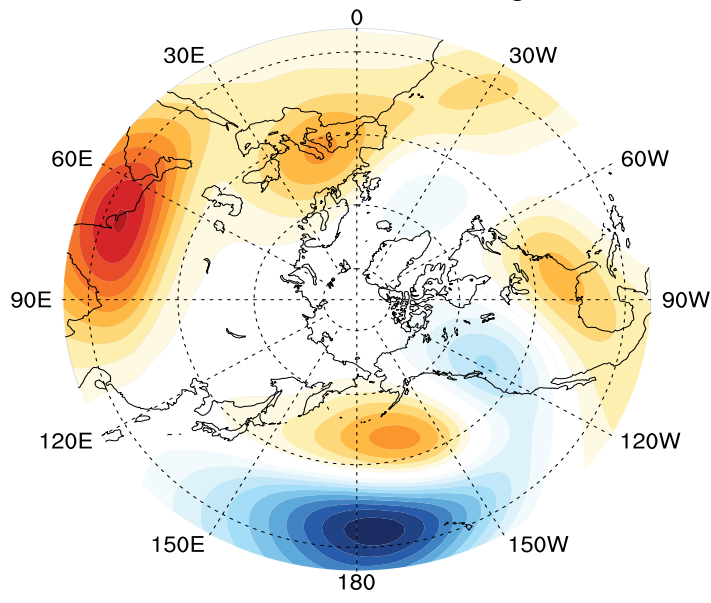
Initial condition

Final condition

# Extratropical initial conditions removed

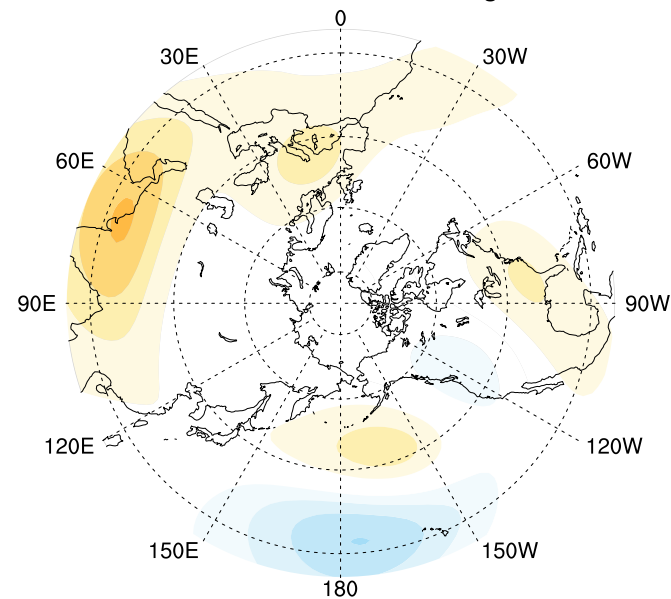
## Unmodified p final PNA

200mb PSI final conditions at lag 15



## Modified p final PNA

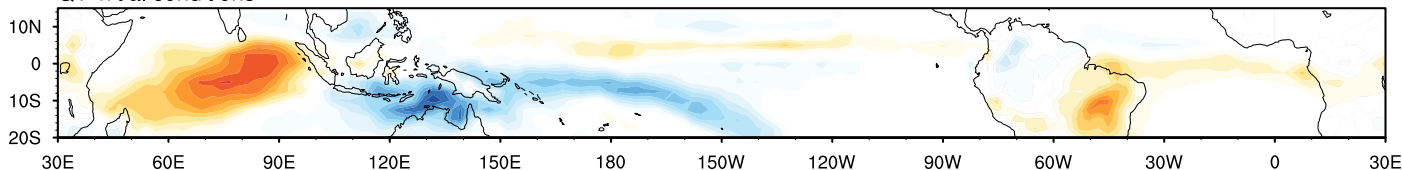
200mb PSI final conditions at lag 15



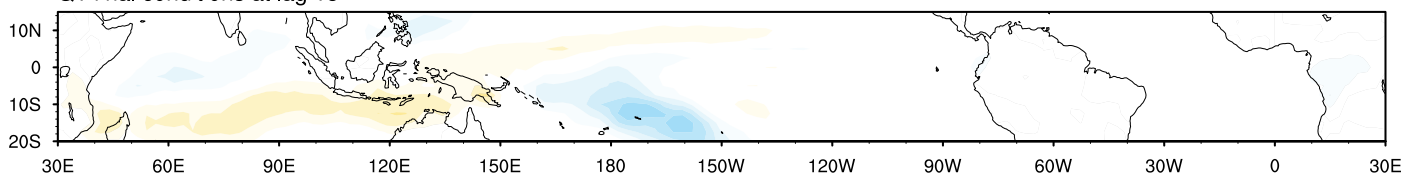
200-hPa  
streamfunction

Q1

Q1 initial conditions

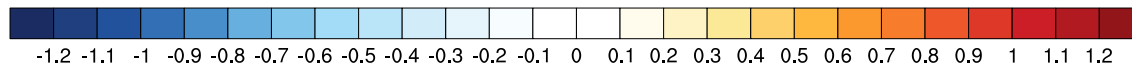


Q1 final conditions at lag 15



Initial condition

Final condition



[K/day]



# Summary

- Linear inverse modeling (LIM) is used to examine the optimal conditions that lead to PNA pattern growth.
- **Unfiltered LIM:** suppressed tropical heating in the SPCZ, ENSO-related heating, and MJO-like heating in the east Indian Ocean optimally lead to PNA pattern growth.
- An **uncoupled LIM** is developed to examine PNA growth outside of ENSO. Optimal PNA growth is from MJO anomalous heating over the east Indian Ocean and suppressed heating over the Maritime continent and SPCZ.
- In the **extratropics**, the optimal initial condition agree with previous studies, including an anticyclonic anomaly over the East Pacific that retrogrades, becoming part of the PNA pattern.
- **Modifying the initial conditions** suggest both tropical heating and the extratropical circulation are important for PNA pattern growth in the uncoupled LIM.