

# The aerosol-cloud-precipitation system: In search of simplicity

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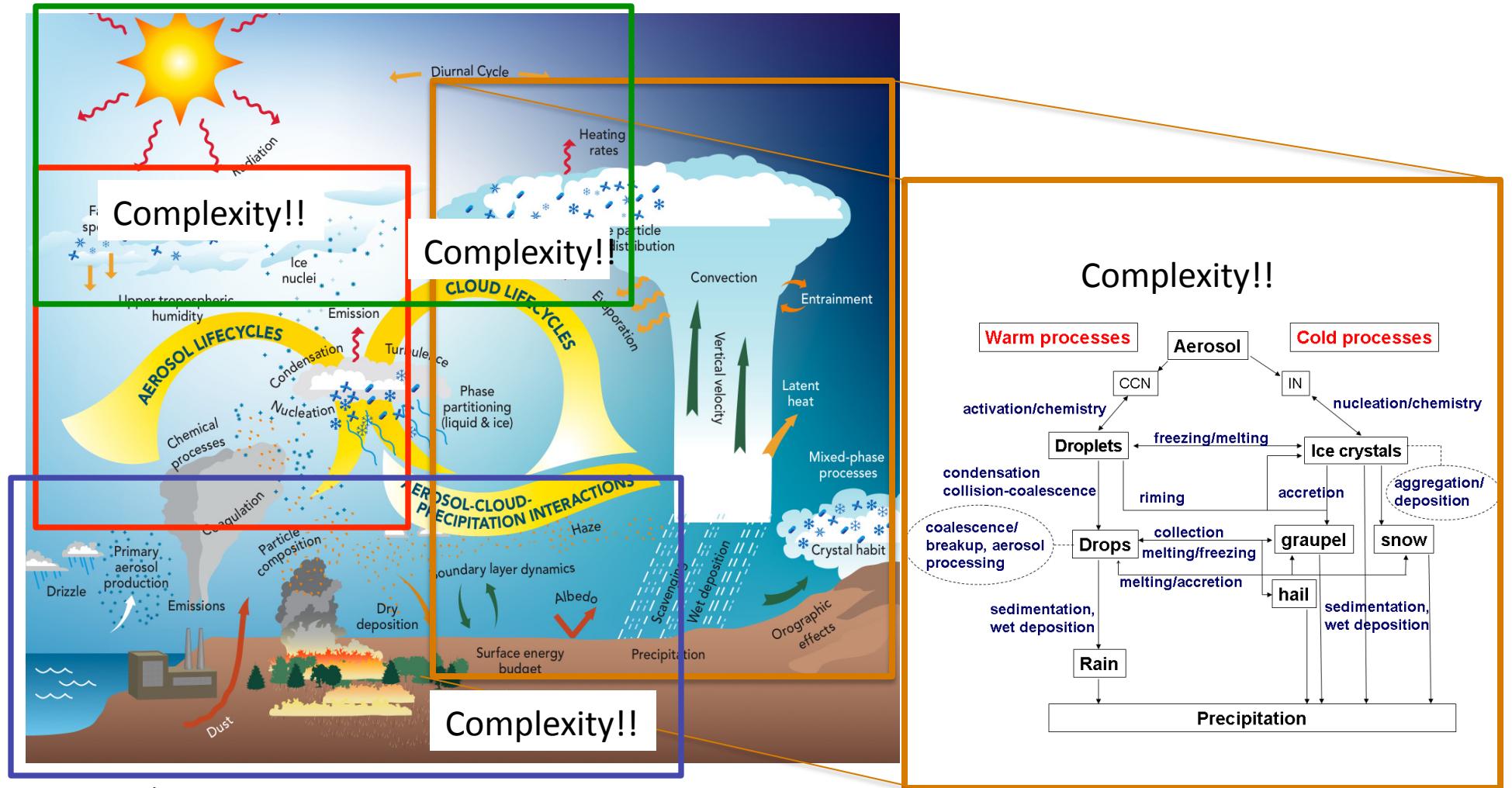
Acknowledgements: Hailong Wang, Huiwen Xue, Alan Brewer

Organizers of WCRP

WCRP October 2011



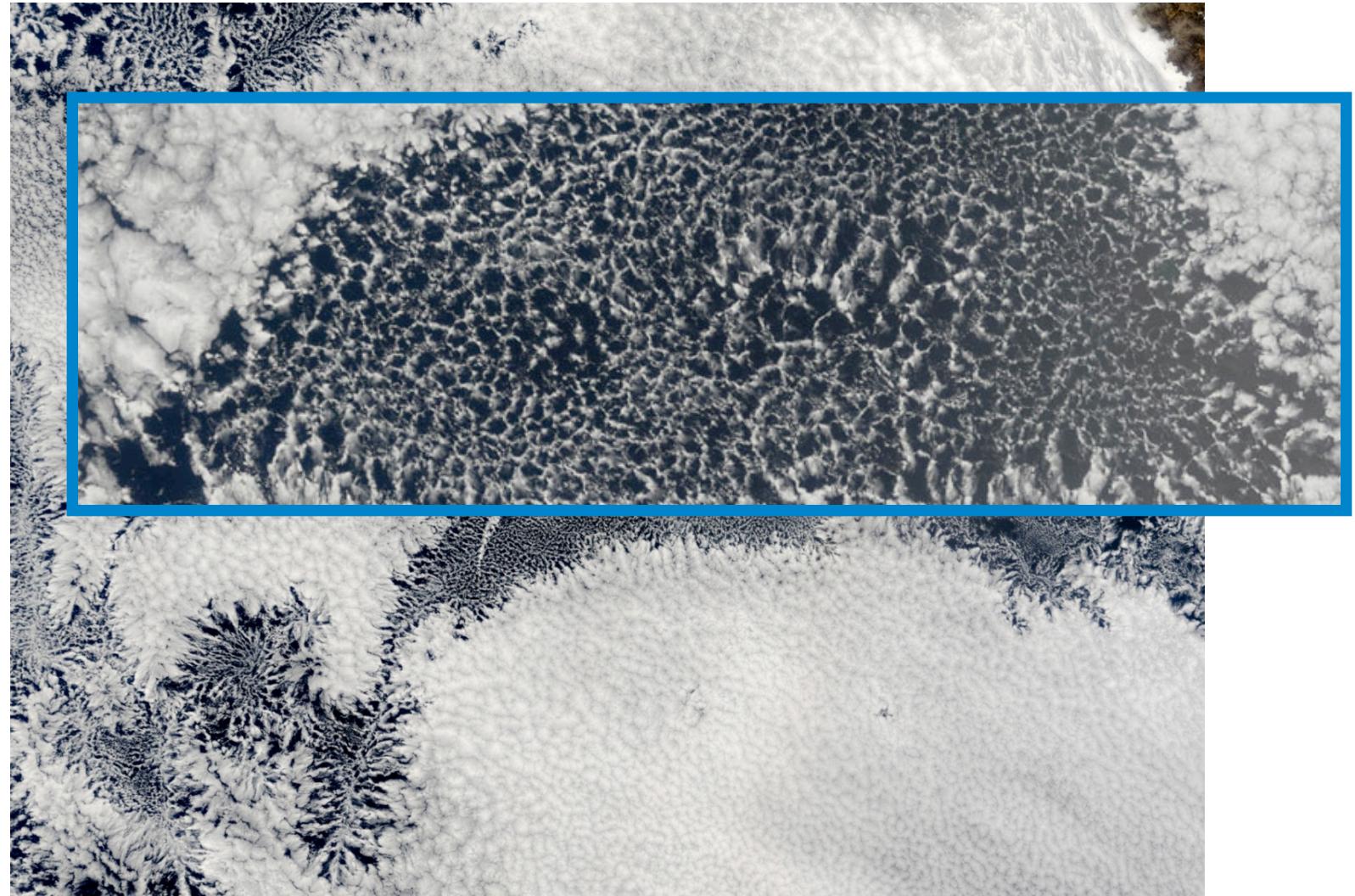
# A complex system: Aerosol-Cloud-Dynamics-Radiation-Land Surface-...



From DOE/ASR Science and Program Plan

- Complexity at a huge range of spatiotemporal scales
- Number of degrees of freedom of this system is staggering
- Important implications for climate

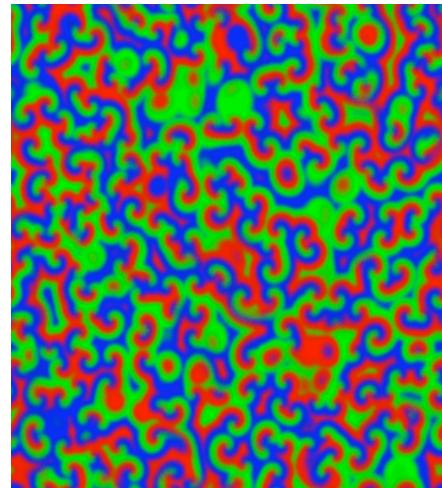
# Mesoscale Cellular Convection



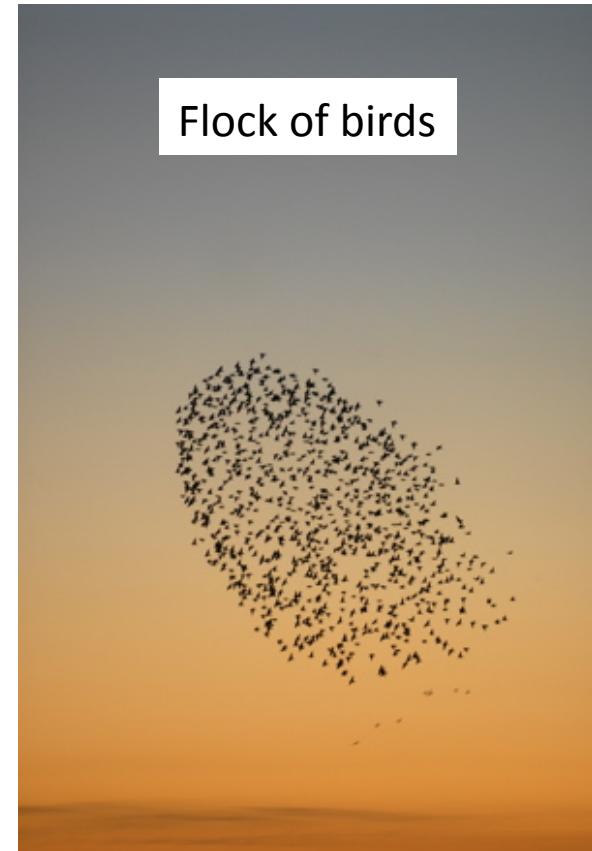
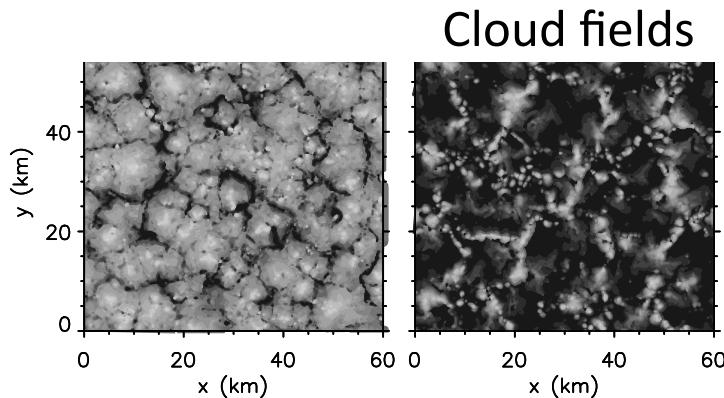
MODIS image, South East Pacific

- *Radiative forcing of the ocean-cloud system*
- *Patterns and emergence in atmospheric systems*

# Patterns and Synchronization in Natural Systems



Oscillatory behavior in  
Belousov-Zhabotinskii  
chemical  
reactions



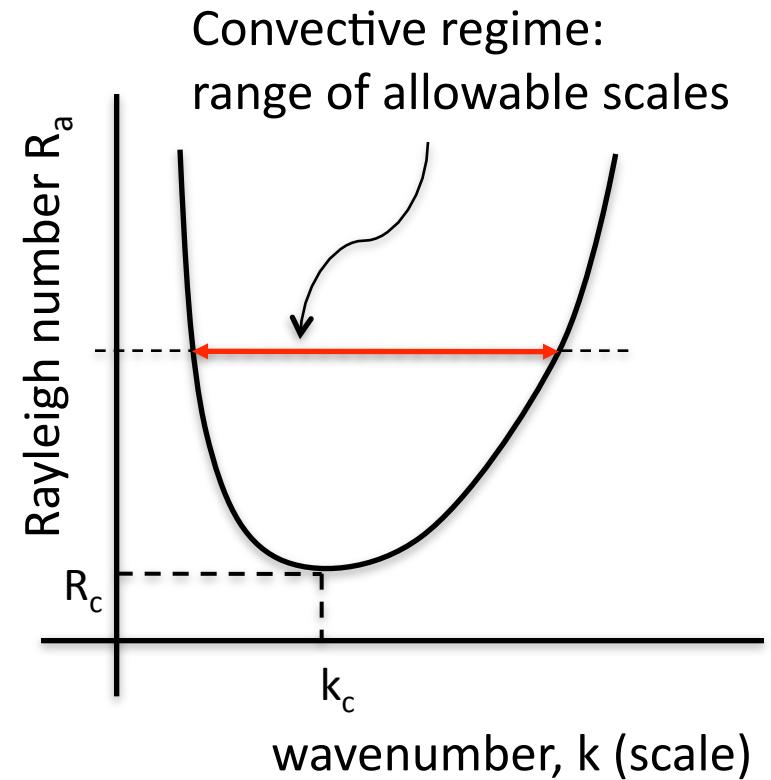
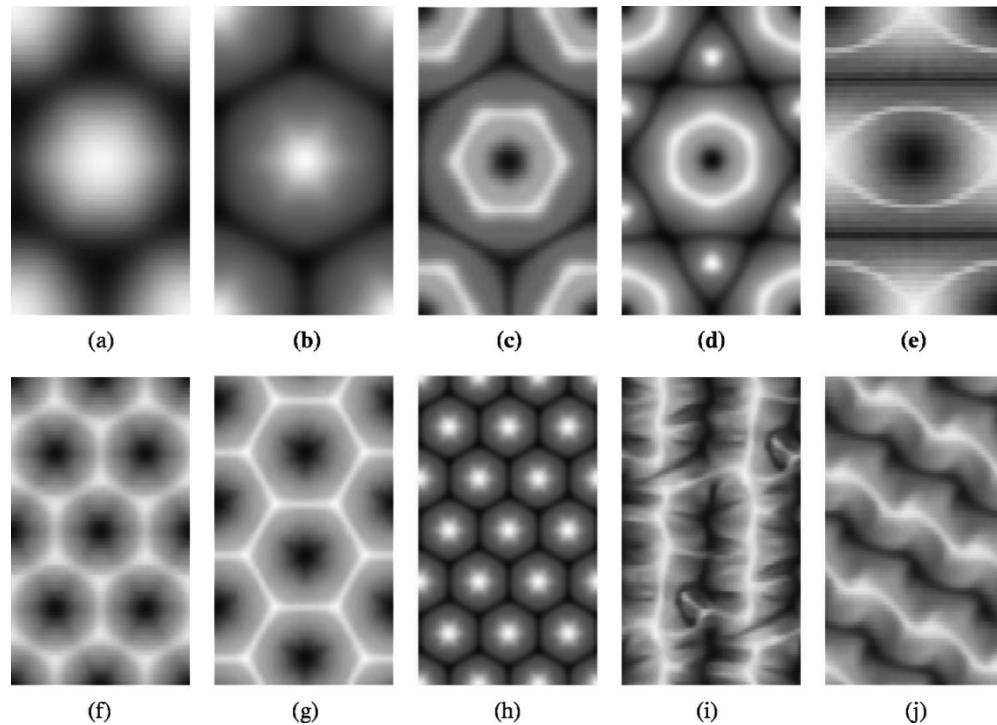
©Miki Meir-Levi

## *“Emergence”*

*System-wide patterns emerge from local interactions between elements that make up the system*

*Implication: Complex problems with huge number of degrees of freedom may be amenable to solution with much more simple set of equations*

# Rayleigh-Bénard Convection

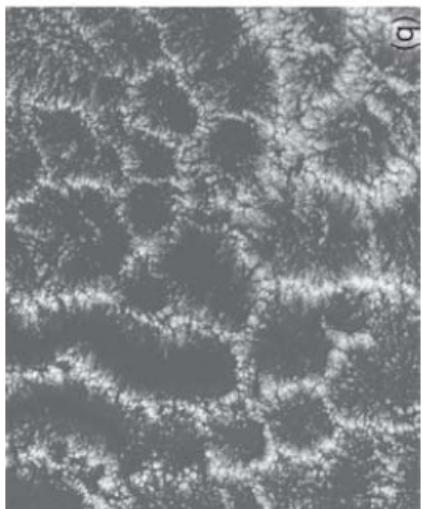


*Controlled lab experiments with different scales:  
Patterns and preferred modes*

Getling and Brausch, Phys. Rev. E 2003

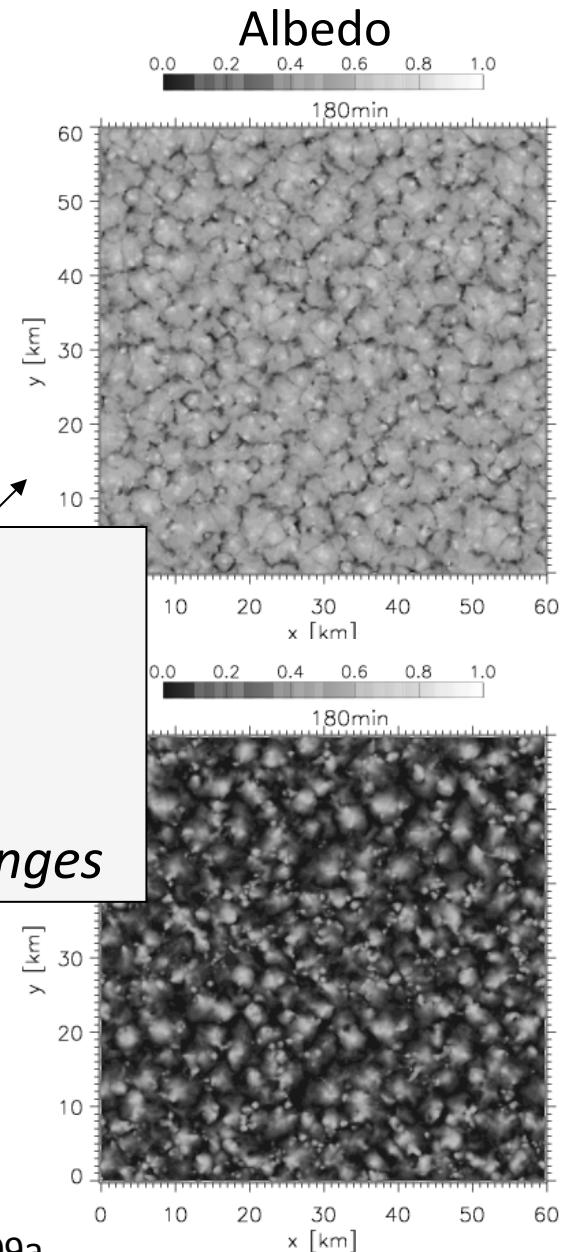
# Aerosol/drizzle selects the state

Albedo

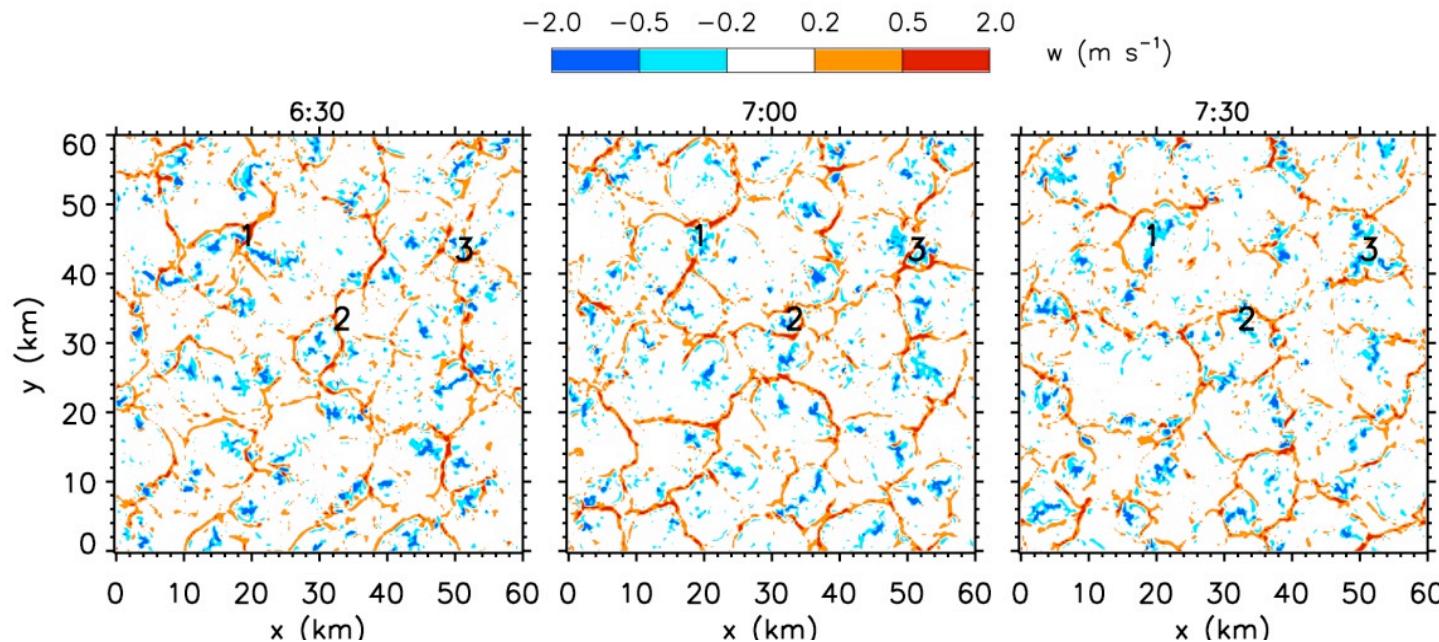


*Onset of drizzle*  
results in (i) Aerosol “selects” the transition state of the system to open-cell convection

(ii) The open state rearranges



# Rearrangement of Open Cells



Orange: Updrafts

Blue: Downdrafts/precipitation

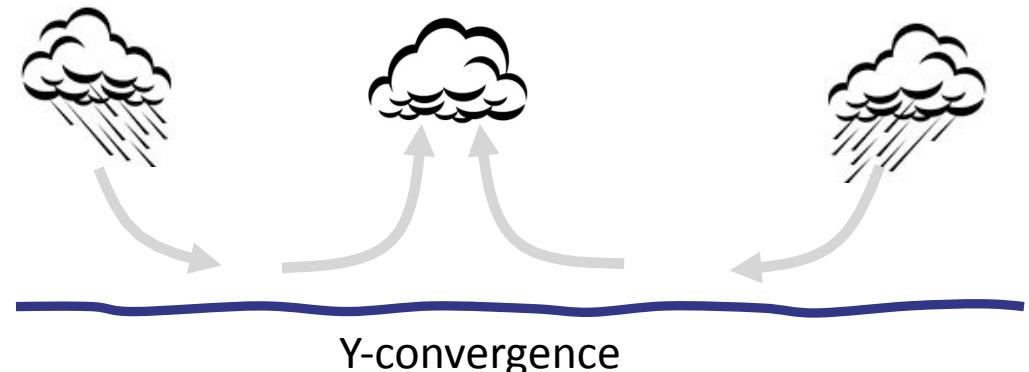
Feingold, Koren, Wang, Xue, Brewer (Nature, 2010)

Y-shaped surface convergence zone  
is region favoured for new convection

↓  
Precipitation is initiated

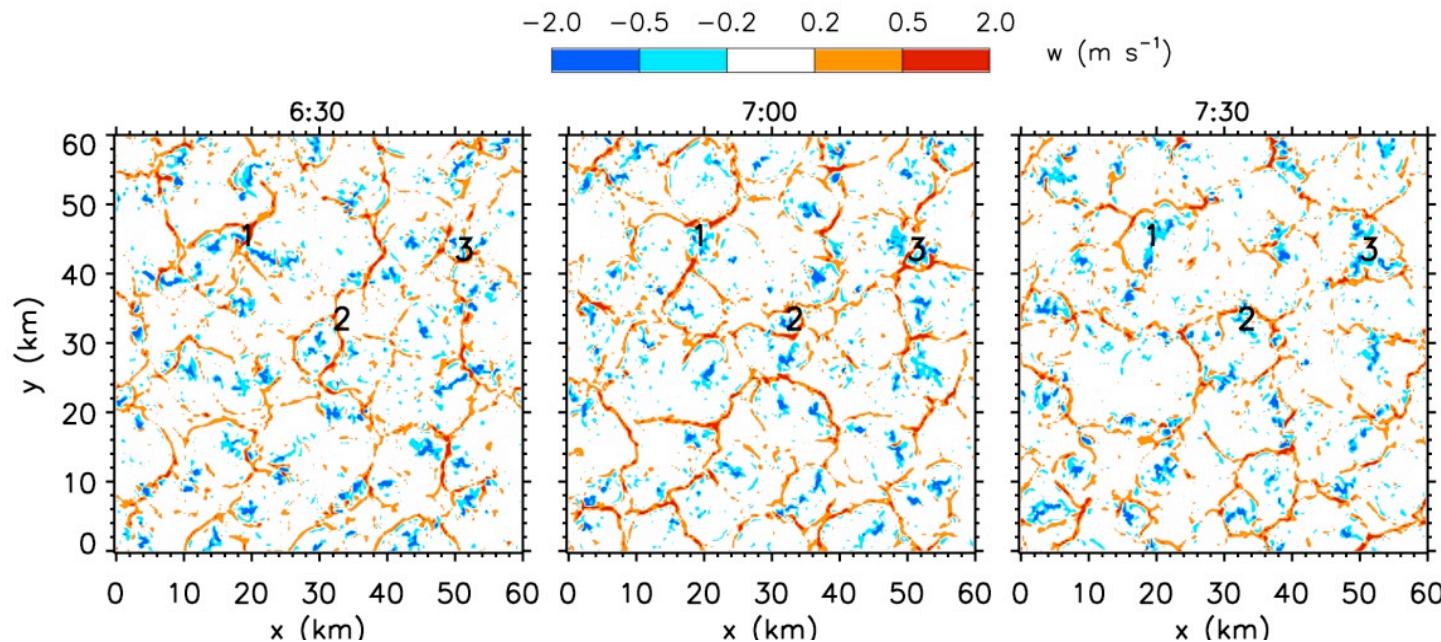
↓  
Downdrafts, opening of cell

↓  
Surface divergence



Buoyancy  $\rightarrow$  cloud  $\rightarrow$  rain  $\rightarrow$  destroys buoyancy

# Rearrangement of Open Cells



No advection

Orange: Updrafts

Blue: Downdrafts/precipitation

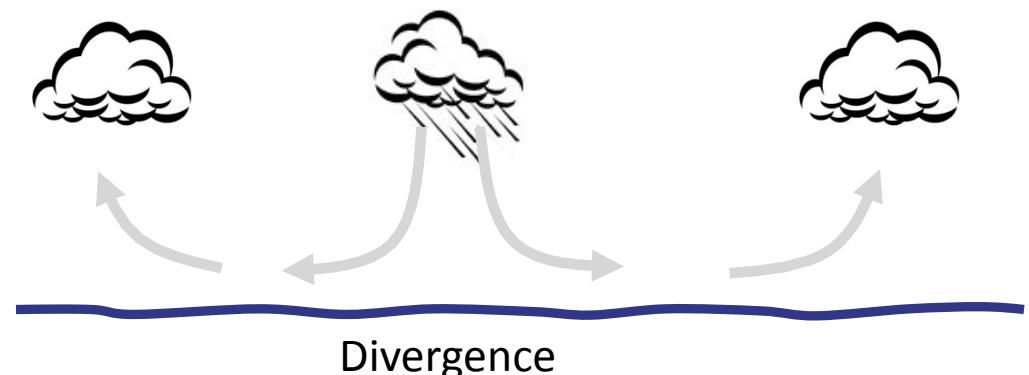
Feingold, Koren, Wang, Xue, Brewer (Nature, 2010)

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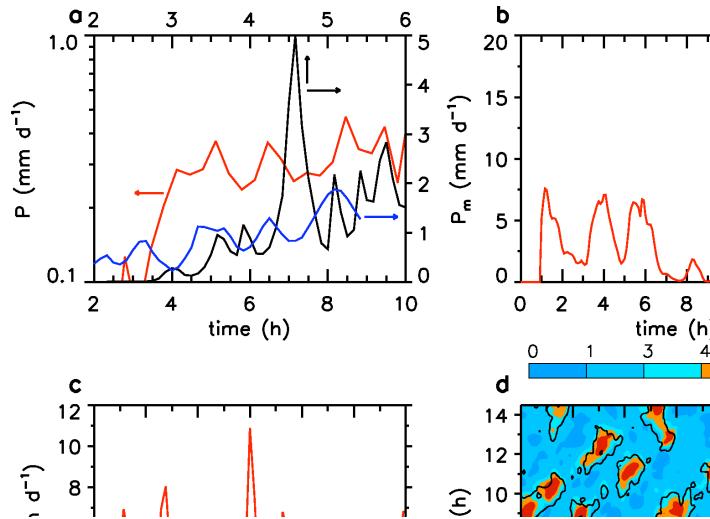
↓  
Downdrafts, opening of cell

↓  
Surface divergence



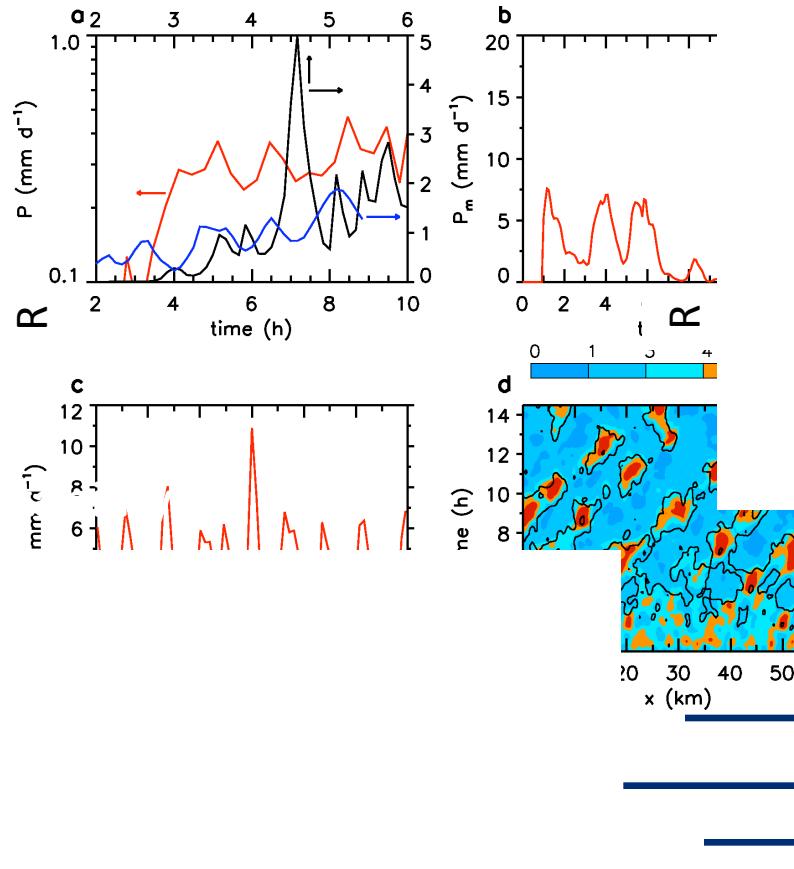
*Emergence due to interaction between outflows*

# Synchronization: Oscillations in Precipitation



3 LES cases:  
**DYCOMS**  
**ATEX**  
**VOCALS**

# Synchronization: Oscillations in Rainrate



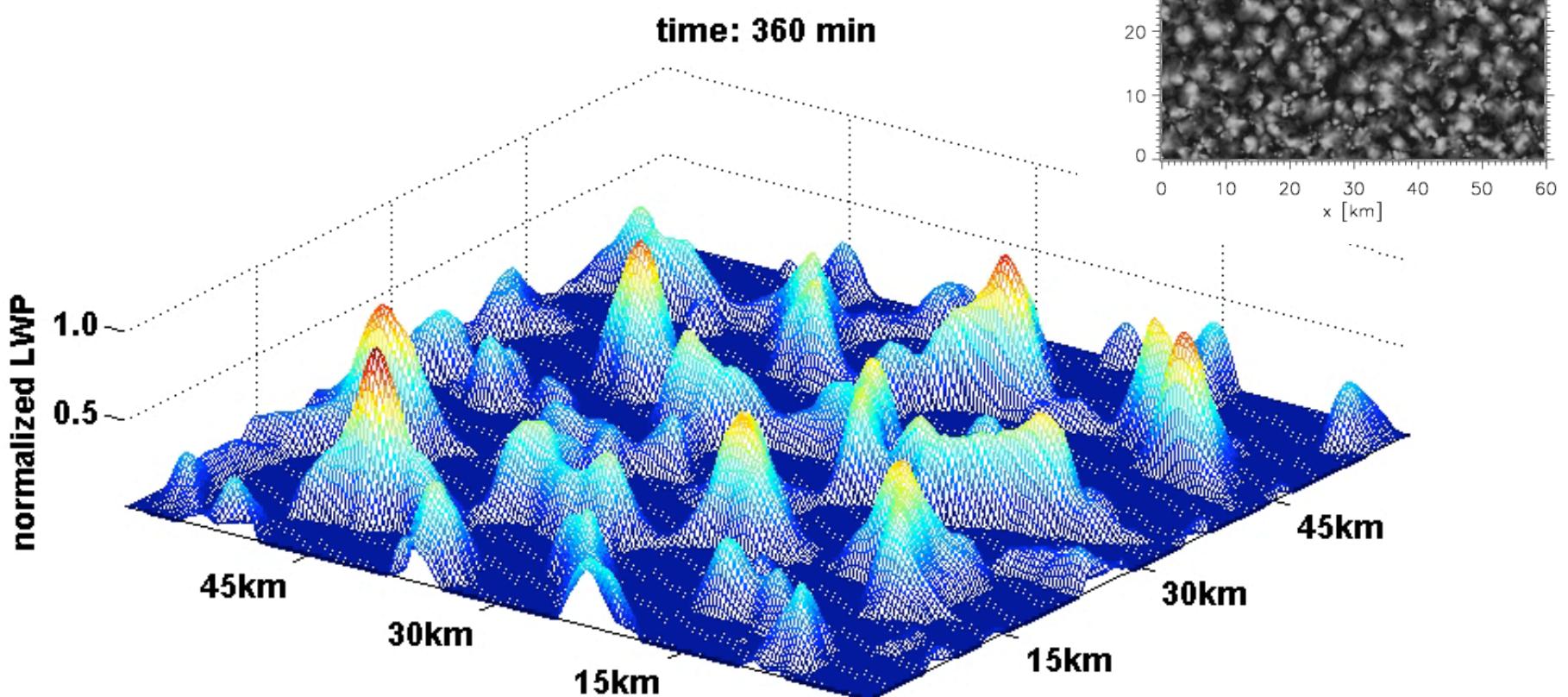
3 LES cases:  
**DYCOMS**  
**ATEX**  
**VOCALS**

Hövmuller diagram

*Shift in rain “grid”*

Colored contours: rain  
Contours: updraft

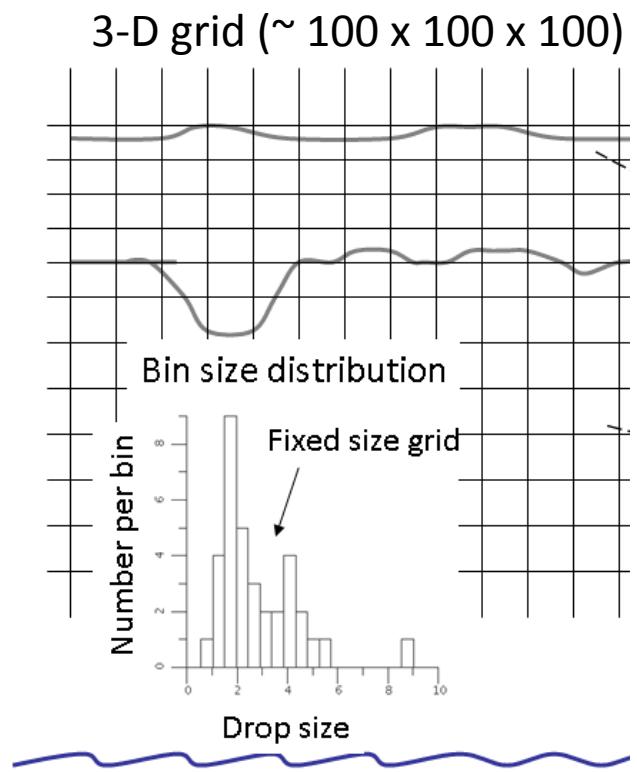
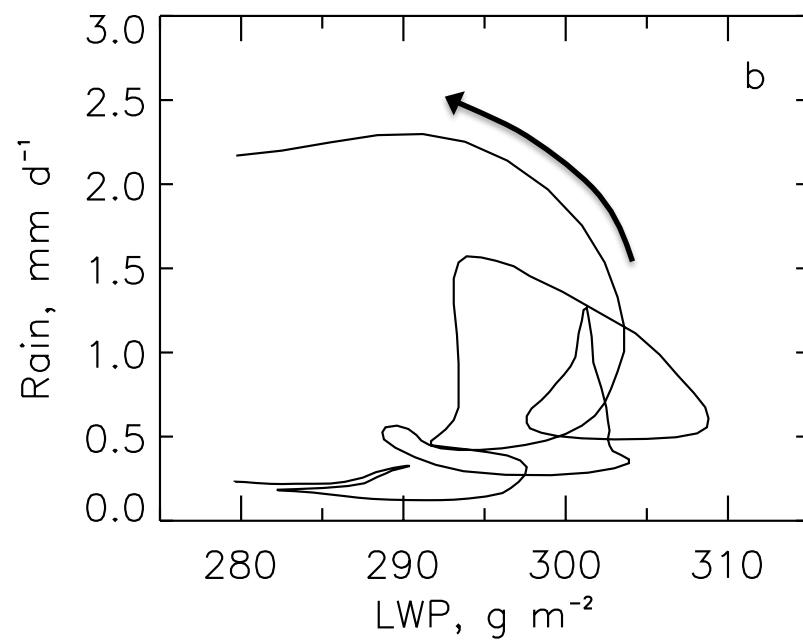
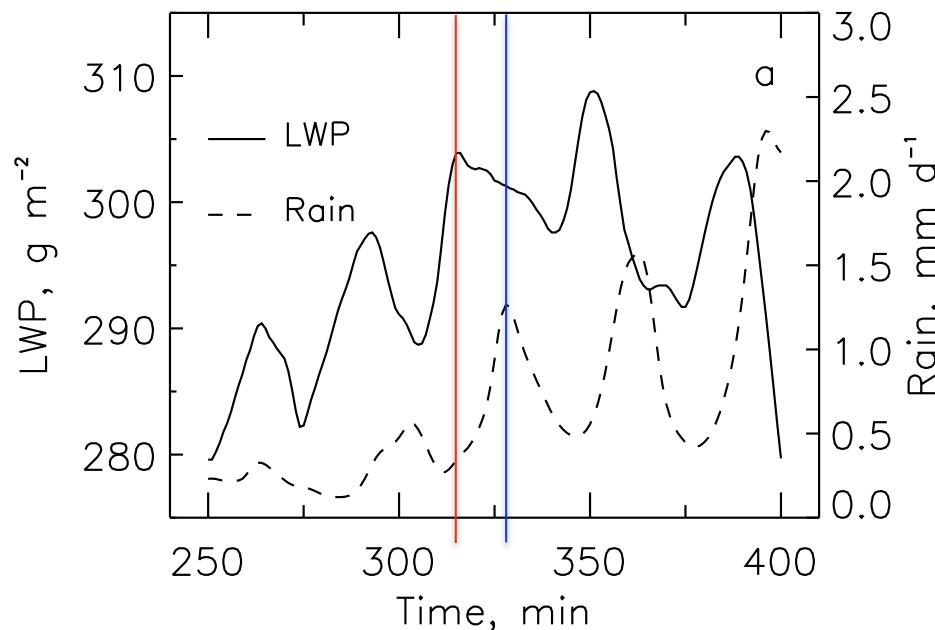
# Synchronization of Coupled Oscillators



Feingold, Koren, Wang, Xue, Brewer (2010)

# **Are Oscillating Patterns Common?**

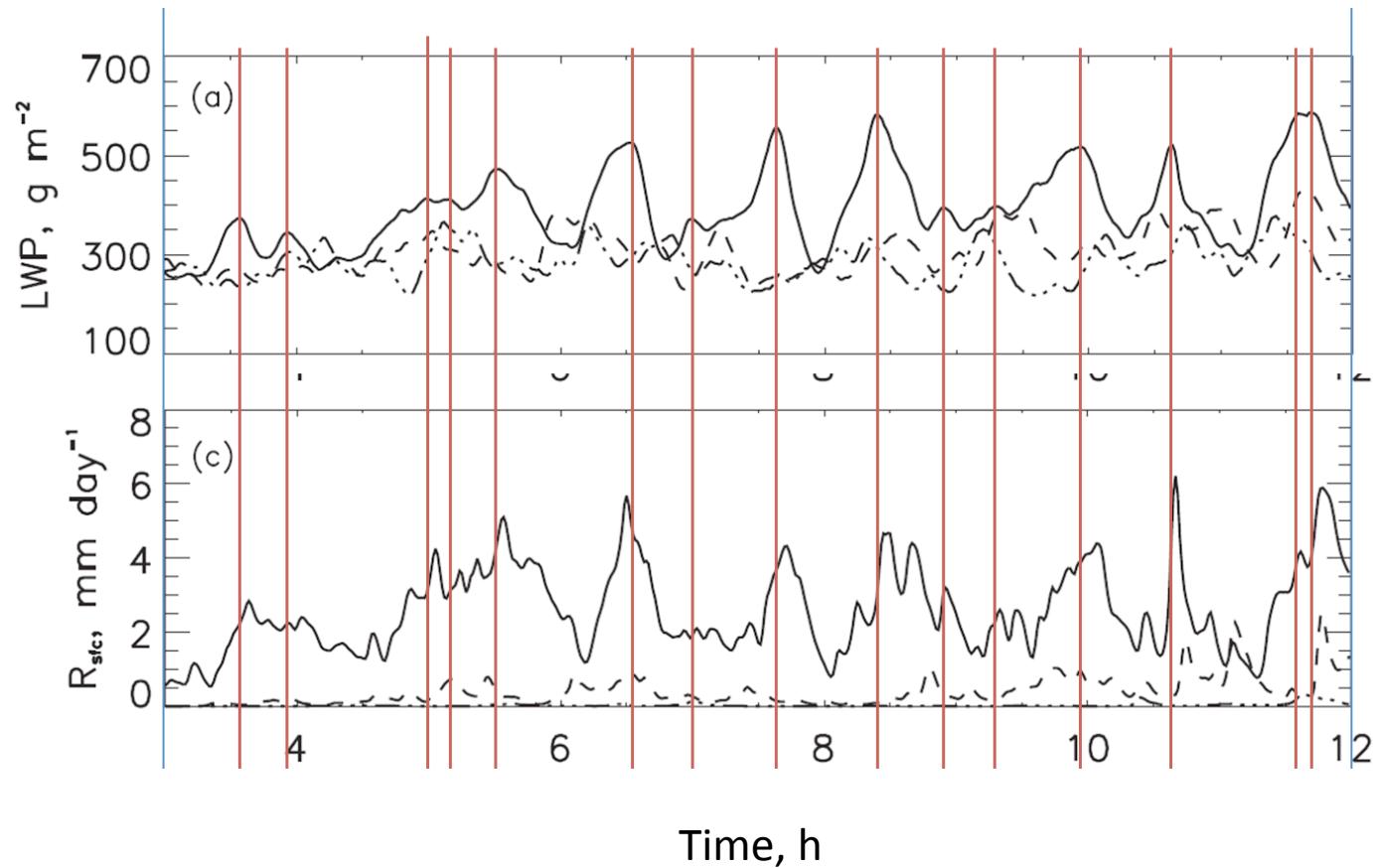
# Large Eddy Simulation of Aerosol-Cloud-Precipitation



Anticlockwise loops in  $R$ ; LWP phase space

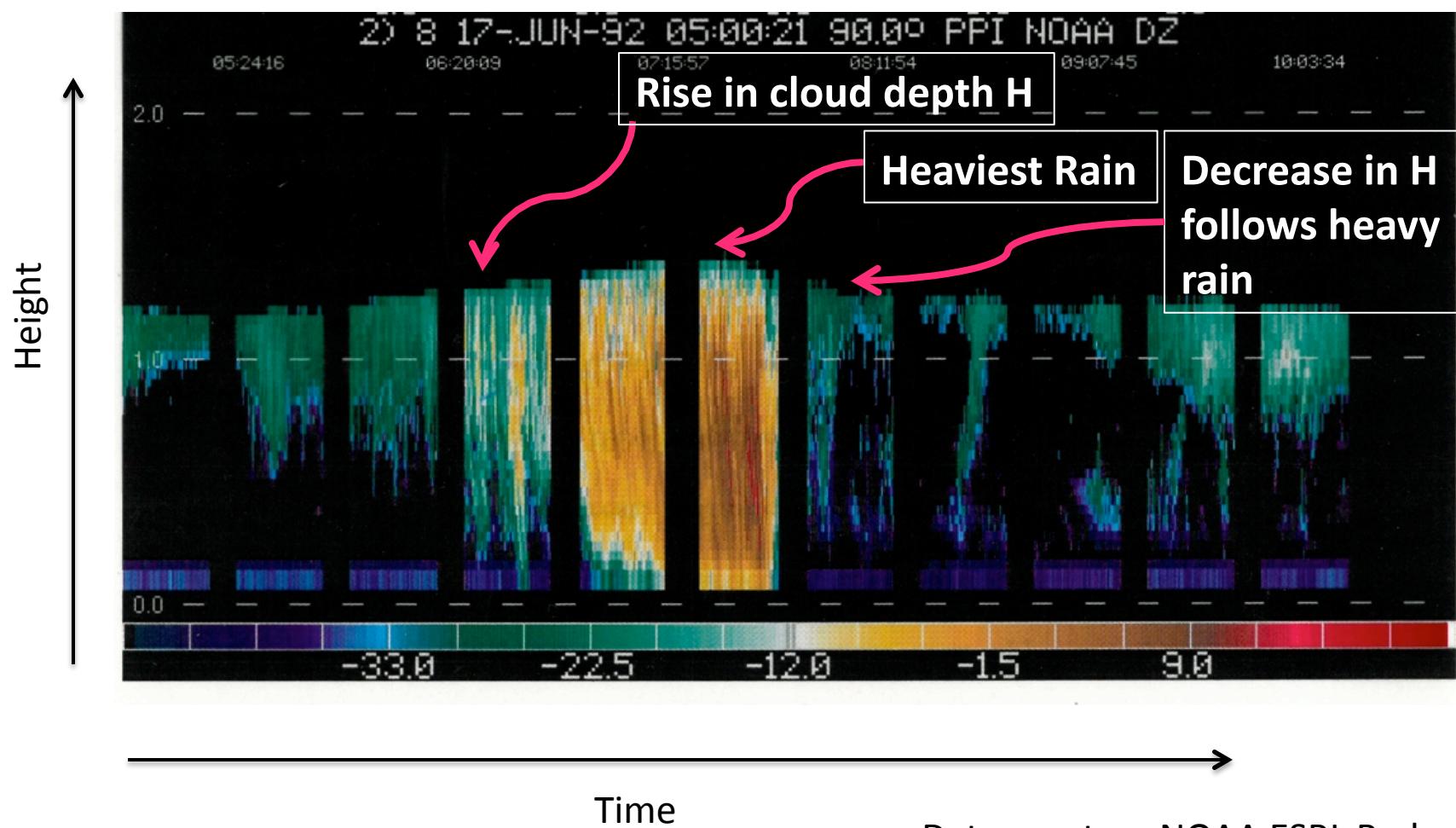
Koren and Feingold 2011, PNAS

## Similar patterns in trade cumulus simulations (RICO)



Jiang et al. 2010

Vertical Profile of Radar reflectivity (a proxy for Rainrate)  
from N. Atlantic (Porto Santo, 1992; ASTEX)



Data courtesy NOAA ESRL Radar Group

# Predator-Prey Model

Lotka-Volterra Equations  
(circa 1926)



$$\frac{dx}{dt} = x(\alpha - \beta y)$$

$$\frac{dy}{dt} = -y(\gamma - \delta x)$$

$x$  = prey

$y$  = predator

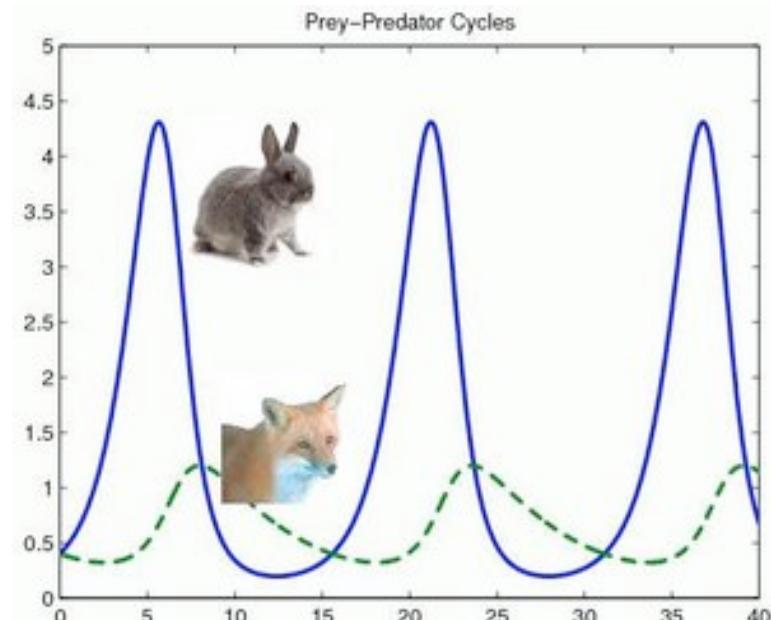
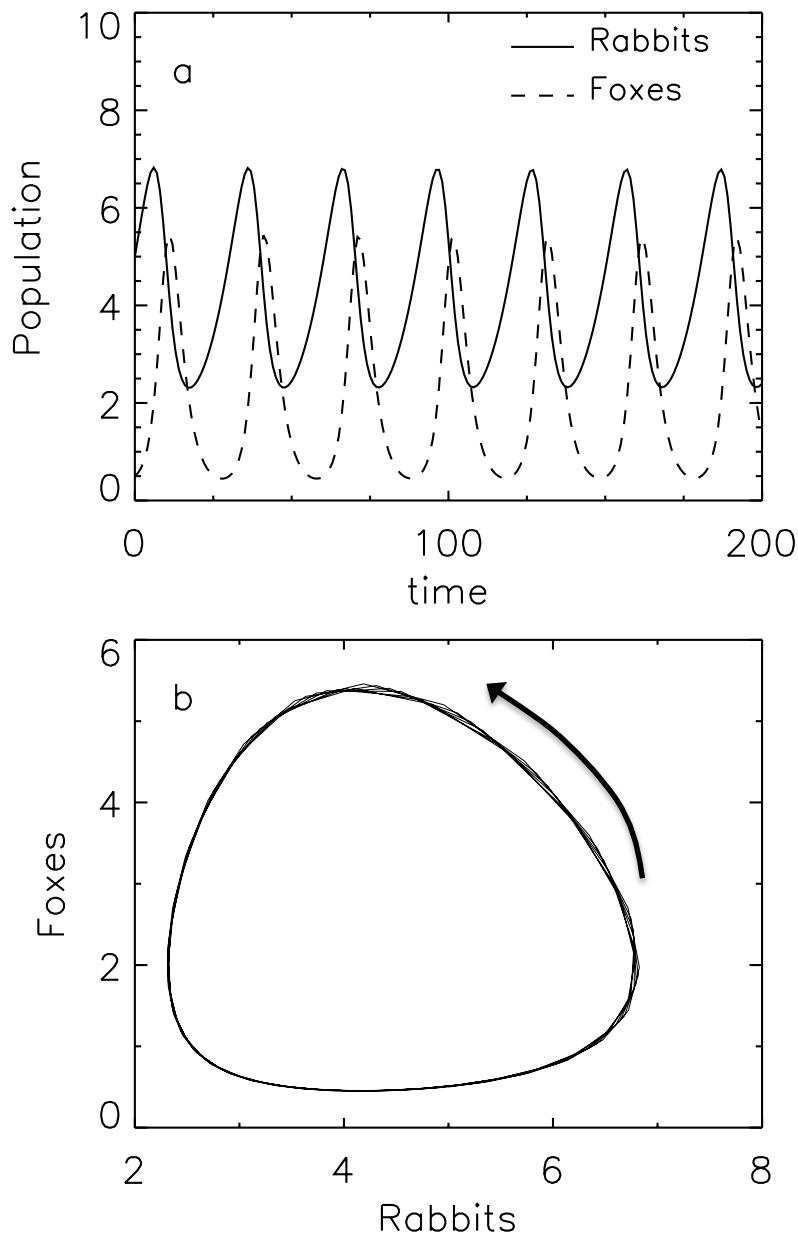


Image courtesy of Wikipedia

4 parameters:  
 $a, b, g, d$

# Predator-Prey Model



Clouds=Rabbits; Rain=Foxes

- Cloud builds up
- Rain follows some time behind
- Rain destroys cloud
- Cloud regenerates  
(met forcing, colliding outflows, etc)

and so on...

*Many possible predator-prey pairs:*

- Rain; Aerosol
- Convection; Instability (Nuber and Graf)
- Droplets; Supersaturation
- Ice; Water (Bergeron-Findeisin)

### 3 simple coupled Balance Equations:

$$\frac{dH}{dt} = \frac{H_0 - H}{\tau_1} + \dot{H}_r(t - T)$$

Cloud depth

$$R(t) = \frac{\alpha H^3(t - T)}{N_d(t - T)}$$

Rainrate

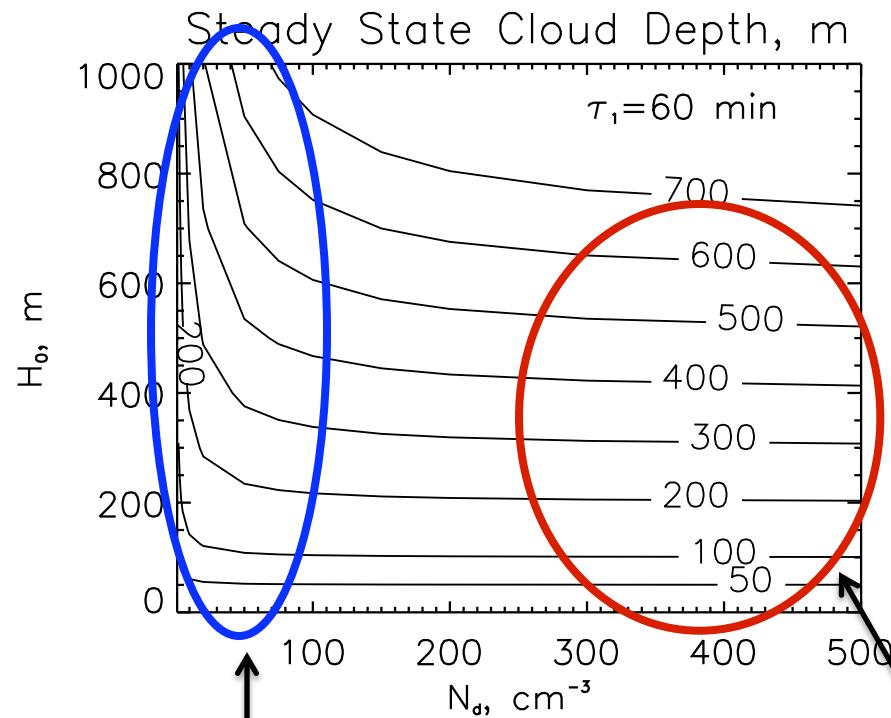
$$\frac{dN_d}{dt} = \frac{N_0 - N_d}{\tau_2} + \dot{N}_d(t - T)$$

Drop conc.

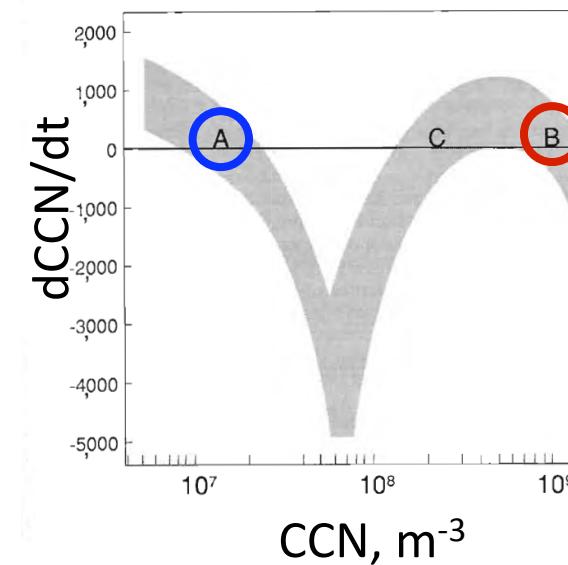
# Steady State Solution to Cloud Depth H

$$\frac{dH}{dt} = \frac{H_0 - H}{\tau_1} + \dot{H}_r(t - T) = 0$$

$$H = \frac{(N_d^2 + 4\gamma\tau_1 N_d H_0)^{\frac{1}{2}} - N_d}{2\gamma\tau_1}$$



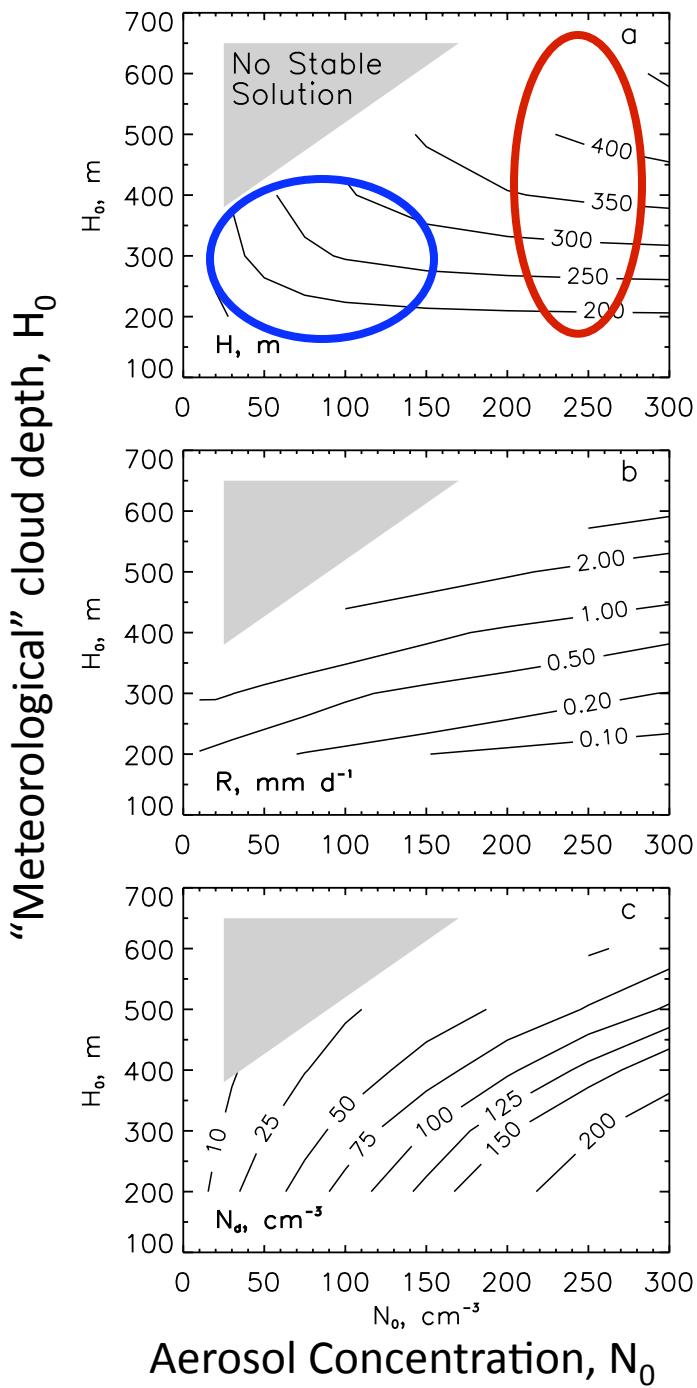
Cloud Depth determined by  
drop concentration  $N_d$



Baker and Charlson, 1990

Cloud Depth determined by  $H_0$

Koren and Feingold 2011, PNAS



# Time-Dependent Steady State Solutions

$$\frac{dH}{dt} = \frac{H_0 - H}{\tau_1} + \dot{H}_r(t - T)$$



Strongly precipitating conditions;  
Aerosol is depleted

$$R(t) = \frac{\alpha H^3(t - T')}{N_d(t - T')}$$

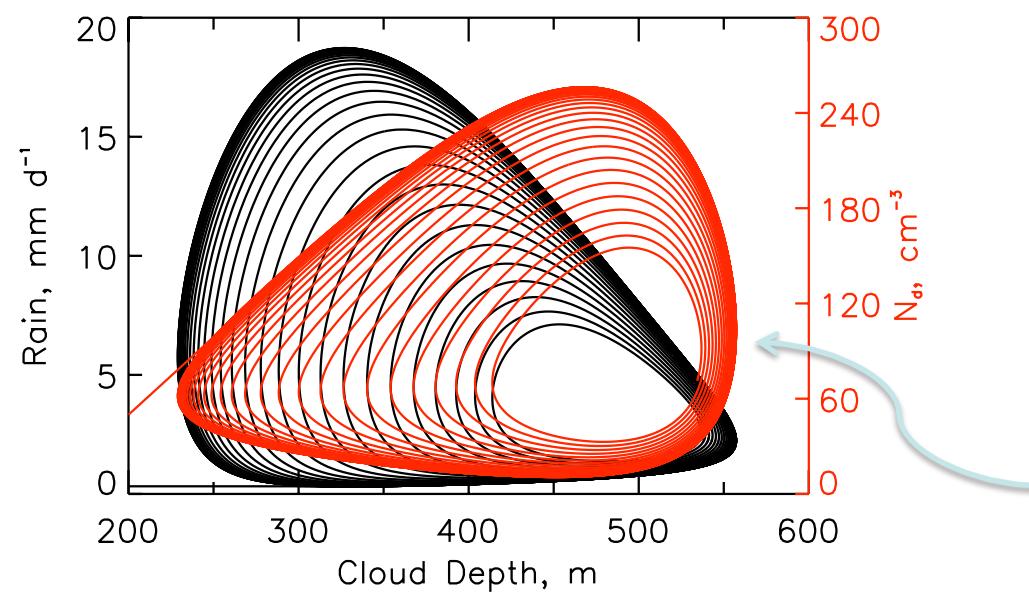
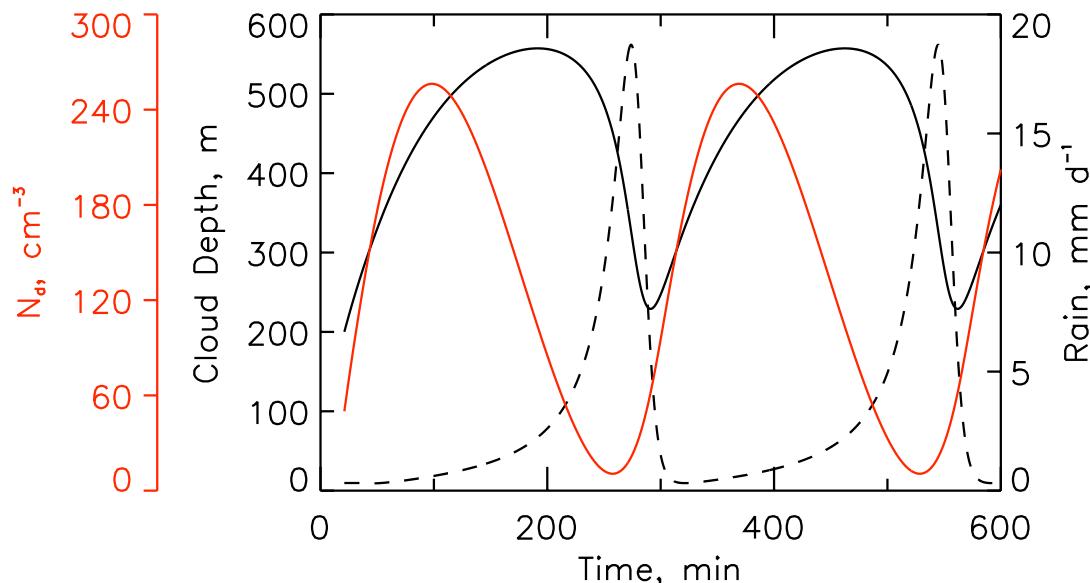
Strong dependence of  $R$  on  $H_o$

$$\frac{dN_d}{dt} = \frac{N_0 - N_d}{\tau_2} + \dot{N}_d(t - T)$$

Higher  $N_o$  supports deeper clouds

$\tau_1 = \tau_2 = 60 \text{ min}$
$T = 10 \text{ min}$

# Oscillating Solutions: No Steady State



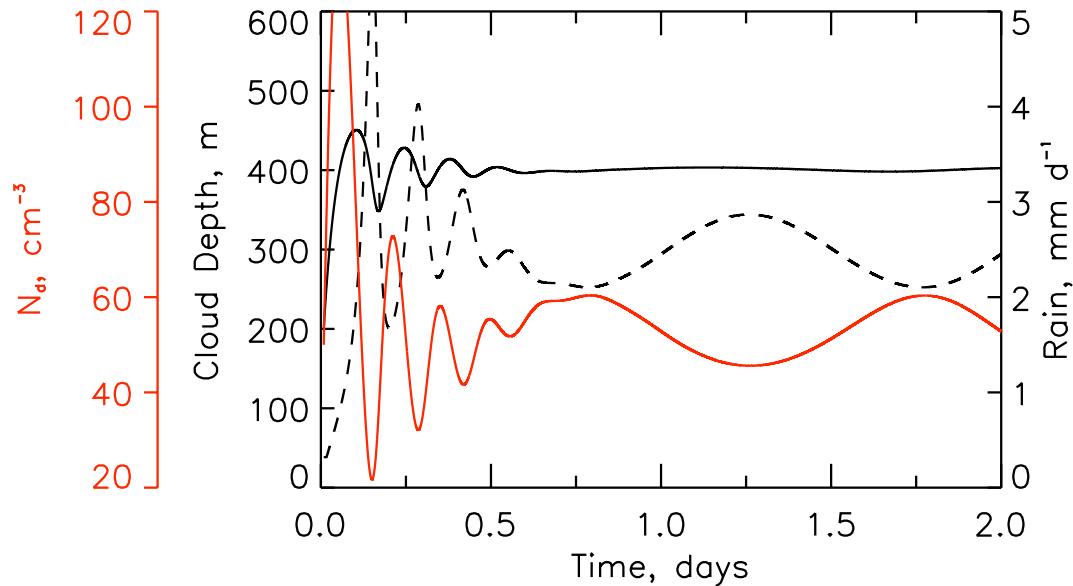
$H_0 = 670 \text{ m}$   
 $N_0 = 515 \text{ cm}^{-3}$   
 $\tau_1 = 80 \text{ min}$   
 $\tau_2 = 84 \text{ min}$   
 $T = 12.5 \text{ min}$

7 day simulation

— H; N  
— H; R

Oscillation around  
a steady state

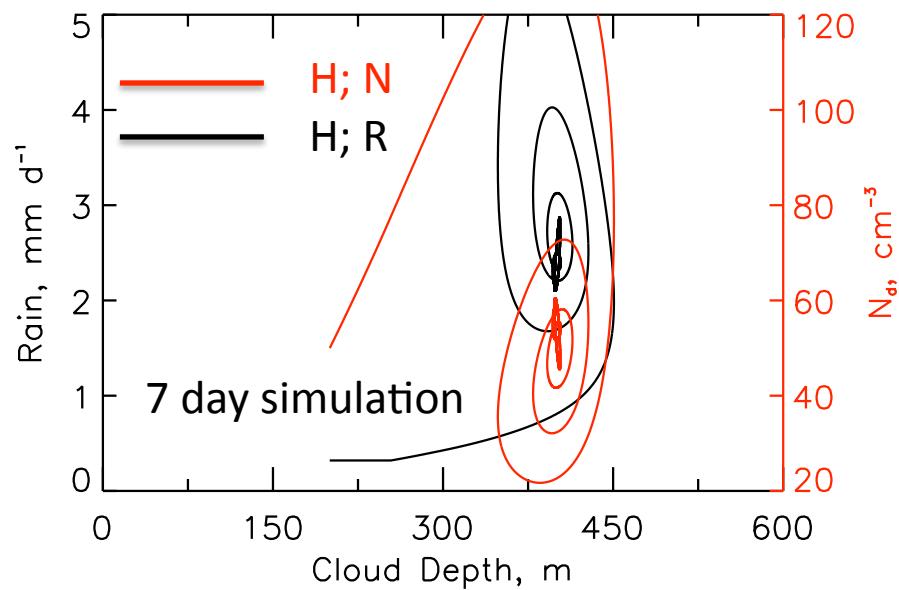
# Forcing at multiple timescales



$$\frac{dH}{dt} = \frac{H_0 - H}{\tau_1} + \frac{\Delta H}{\tau_2} + \dot{H}_i(t - T)$$

$\tau_1 = 1$  h (microphysics)

$\tau_2 = 24$  h (largescale forcing)



# Robustness of the System

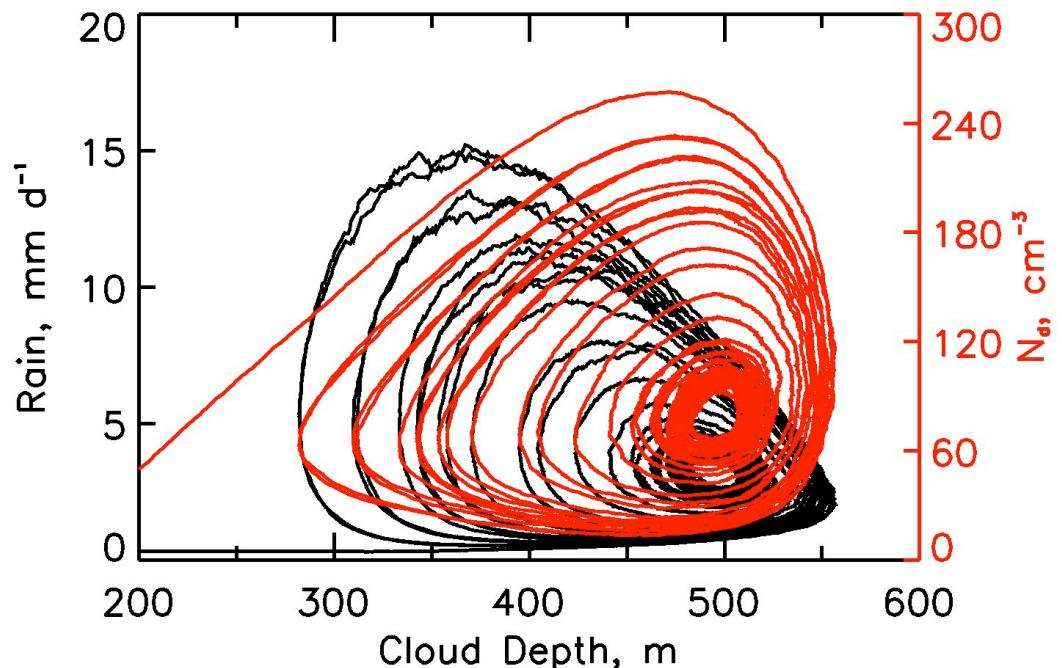
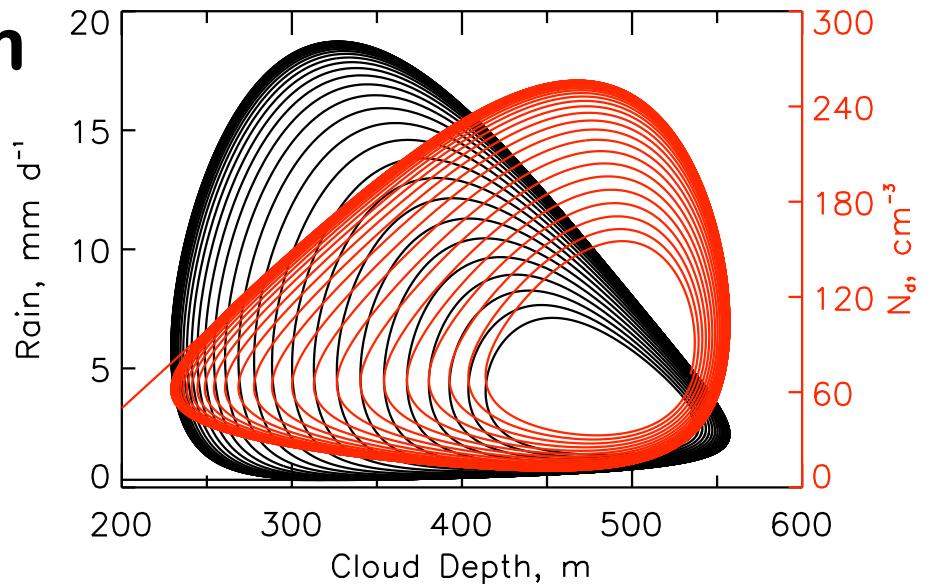
*How stable are the stable states?*

*Small perturbations strengthen the resilience of the state*

$\pm 50\%$  perturbations to  $H_0$  and  $N_0$  every second: Solutions are robust

*Small perturbations strengthen the resilience of the state;*

*Large enough perturbations will lead to collapse*



# Summary

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- *Emergence*
  - Local interactions result in system-wide order
  - convergence of precipitating outflows
- *Self-organization*
  - Aerosol/drizzle can select open/closed cellular state
- *Synchronization*
  - Local interactions: synchronized rain, oscillations in open-cell state
- *The predator-prey problem*
  - Coupled oscillations in Cloud-Rain “Populations”
  - Bifurcation
  - Interactions at multiple timescales
- *Can we exploit emergence to represent complex systems?*
  - (E.g. Mapes 2011; Bretherton et al. 2010)