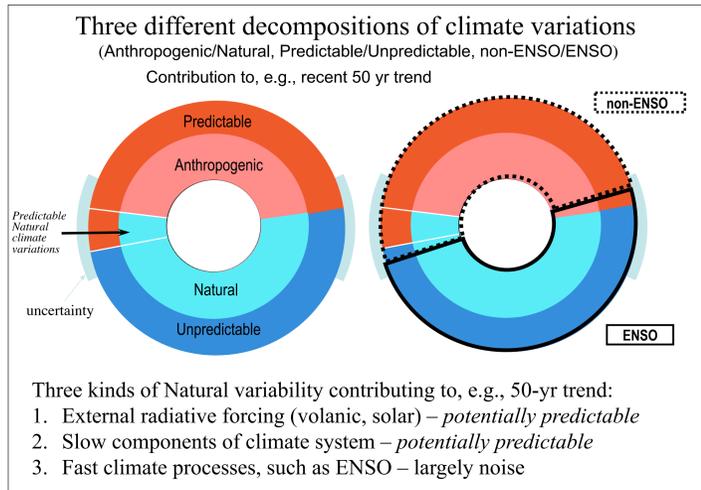


# Removing ENSO-related Variations from the Climate Record

Gilbert P. Compo and Prashant D. Sardeshmukh  
*Climate Diagnostics Center, CIRES, University of Colorado, Boulder, CO*  
*Physical Sciences Division, Earth System Research Laboratory, NOAA, Boulder, CO*

## Introduction



The El Niño Southern Oscillation (ENSO) phenomenon has a rather long low-frequency tail, which contributes to “ENSO-like multi-decadal variability” and trends. This is mostly climate noise.

1. How should one identify ENSO-related variations?
2. How should one remove such ENSO-related variations from the climate record?
3. What do the trends and multi-decadal variations look like after doing this?

## 1. How should one identify ENSO-related variations?

Tropical SST state vector :  $\mathbf{x}(t) = \mathbf{x}_e(t) + \mathbf{x}_n(t)$

ENSO part      Non-ENSO part

Rest of climate state vector :  $\mathbf{y}(t) = \mathbf{y}_e(t) + \mathbf{y}_n(t)$

$= \mathbf{A} \mathbf{x}_e(t) + \mathbf{y}_n(t)$

**Note !**  $\mathbf{x}_e$  is not necessarily orthogonal to  $\mathbf{x}_n$ , nor is  $\mathbf{y}_e$  to  $\mathbf{y}_n$

Non-orthogonality implies that one cannot estimate  $\mathbf{A}$  by regressing  $\mathbf{y}(t)$  on  $\mathbf{x}_e(t)$ .

Almost all previous studies have assumed orthogonality, even though there is no physical reason to do so.

### Some difficulties with traditional approaches:

1. Defining  $\mathbf{x}_e$  as the band-pass filtered  $\mathbf{x}$  in the 2 to 6-yr band assumes that **all** of the SST variability in this band, and none outside it, is ENSO-related.
2. Defining  $\mathbf{x}_e$  in terms of an SST index in grid space (such as a Nino3.4 index) implies that there can never be a non-ENSO part  $\mathbf{x}_n$  in that index *by definition*, for instance, one can never have a “global warming” signal in Nino3.4
3. Defining  $\mathbf{x}_e$  in terms of an SST index in EOF space (such as the 1st PC) has the same problem. In addition, it assumes that  $\mathbf{x}_n$  is orthogonal to  $\mathbf{x}_e$ .

### Define ENSO from the dynamical operator $\mathbf{L}$ governing Tropical SST evolution

(Penland and Sardeshmukh 1995; Penland and Matrosova 2006):

$$\mathbf{x}(t+\tau) = \exp(\mathbf{L}\tau) \mathbf{x}(t) + \text{noise}(t)$$

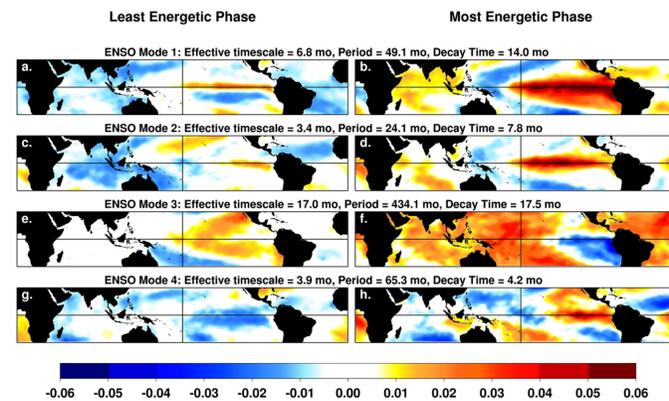
estimating  $\mathbf{L}$  from the lag covariances  $\mathbf{C}(t) = \langle \mathbf{x}(t)\mathbf{x}^T(t) \rangle$  of monthly SST in the HadISST dataset (1949-2004) at lag 0 and lag  $\tau_0 = 3$  months as

$$\mathbf{L} = \frac{1}{\tau_0} \ln \{ \mathbf{C}(\tau_0) \mathbf{C}(0)^{-1} \}$$

## 2. How should one remove ENSO-related variations from the climate record?

First, define ENSO as the 4 dynamical eigenmodes of  $\mathbf{L}$  that contribute most to the observed growth and decay of events.

What do these modes of  $\mathbf{L}$  look like?



(left) Least energetic and (right) most energetic phases of the four dynamical ENSO modes used for defining the ENSO-related tropical SST variations. Each mode's effective time scale is indicated. Each mode evolves from (left) the least energetic phase **a** to (right) the most energetic phase **b**, then to **-a**, and then to **-b** with the indicated period while decaying with the indicated decay time scale. The **a** phase is normalized to unity in the left panel. Note that the **a** and **b** phases of each mode are spatially orthogonal to each other by construction.

Second, project these ENSO modes onto the observed Tropical SST record to form  $\mathbf{x}_e$ . Then, extend ENSO to extratropical SSTs  $\mathbf{y}_e$  using an “Atmospheric Bridge”  $\mathbf{A}$ . Finally, remove both from original monthly SST record.

**Tropical SSTs :**  $\mathbf{x}(t+\tau) = \exp(\mathbf{L}\tau)\mathbf{x}(t) + \varepsilon$  over short intervals  $\tau$  (~ several seasons)

$$\mathbf{x}(t) = \mathbf{x}_e(t) + \mathbf{x}_n(t)$$

$$\mathbf{x}_e(t) = \sum_{i=1,4} \alpha_i(t) \mathbf{u}_i = \sum_{i=1,4} [\mathbf{v}_i^T \mathbf{x}(t)] \mathbf{u}_i$$

where  $\mathbf{u}_i$  are the 4 ENSO-relevant eigenvectors of  $\mathbf{L}$  and  $\mathbf{v}_i$  are the corresponding adjoint eigenvectors

**Extratropical SSTs :**  $\mathbf{y}(t) = \mathbf{y}_e(t) + \mathbf{y}_n(t)$

$$\mathbf{y}_e(t) = \mathbf{A} \mathbf{x}_e(t)$$

$$\mathbf{A} = \langle \mathbf{y}_e(t) \mathbf{x}_e^T(t) \rangle > \langle \mathbf{y}_n(t) \mathbf{x}_e^T(t) \rangle^{-1}$$

where  $\mathbf{x}_e$  and  $\mathbf{y}_e$  are band-pass filtered time series of  $\mathbf{x}$  and  $\mathbf{y}$  in the 2 to 72-month period band.

## 4. Conclusions

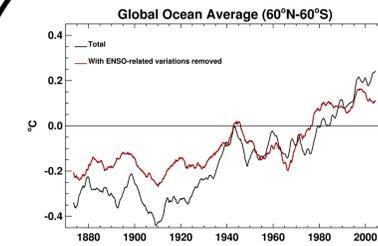
1. Identifying and removing ENSO-related variations by using simple regressions on any single ENSO index can be problematic.
2. **ENSO is not a number.** It is an evolving dynamical process.
3. We identify ENSO-related SST variations with the projection on the 4 most important dynamical SST eigenmodes involved in the growth and decay of ENSO events over several seasons.
4. Removing ENSO-related variations has a large effect on SST trends, up to 40% of the total trend in globally-averaged ocean temperatures. There is a strong cooling trend in the eastern equatorial Pacific Ocean.
5. The residual SST data (that is, data from whom the ENSO component has been removed) reflect a combination of anthropogenic, naturally forced, and coherent internal multi-decadal variability.
6. The 1st EOF of the residual SST data has a general “global warming” structure, but also a pronounced cooling in the eastern equatorial Pacific.
7. The 2nd EOF is strongly suggestive of a multi-decadal zonally symmetric Tropical-Extratropical SST seesaw (TESS). Is this forced or natural variability?

References: Compo, G.P., and P.D. Sardeshmukh, 2010: *Removing ENSO-related variations from the climate record*. *J. Climate*, 23, 1957-1978. DOI: 10.1175/2009JCLI2735.1.

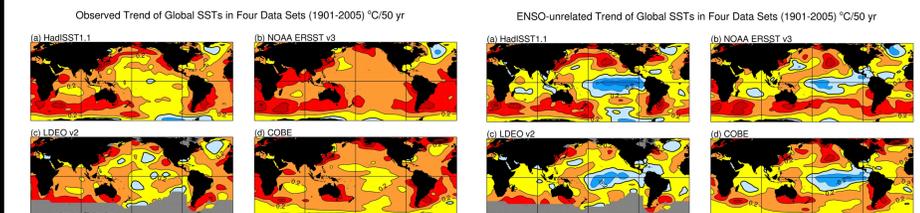
Penland, C., and P.D. Sardeshmukh, 1995: *The optimal growth of tropical sea surface temperature anomalies*. *J. Climate*, 8, 1999-2024.

Penland, C., and L. Matrosova, 2006: *Studies of El Niño and interdecadal variability in tropical sea surface temperatures using a nonnormal filter*. *J. Climate*, 19, 5796-5815.

## 3. What do trends look like after removing ENSO?

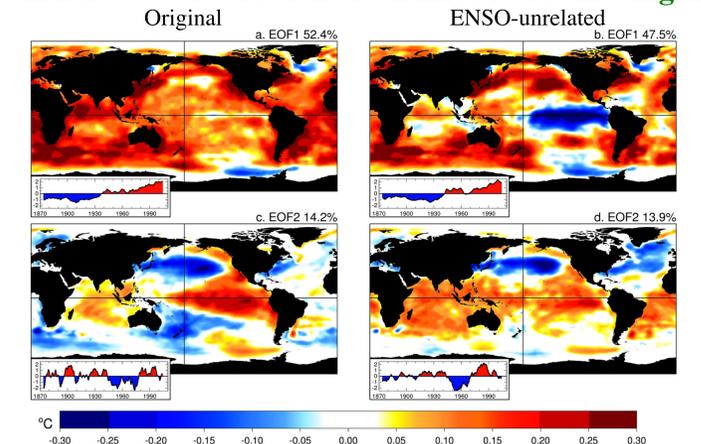


Time series of the global ocean average surface temperature anomaly (black curve) and its ENSO-unrelated component (red curve). A 10-yr running mean has been applied to both series. Anomalies are relative to a 1949–2004 climatology. **The ENSO-unrelated trend is ~60% of the original trend.**



(left 4 panels) Global maps of observed linear trends and (right 4 panels) after ENSO has been removed over 1901–2005 from four different SST datasets: (a) HadISST v1.1, (b) NOAA ERSST version 3, (c) LDEO SST version 2, and (d) COBE SST. Contour interval is 0.2°C change per 50 years. The zero contour is thickened.

## What do multidecadal variations look like after removing ENSO?



(left) The two leading Empirical Orthogonal Functions (EOFs) and associated principal components (PCs) (inset) of 5-yr running mean SST anomalies from the 1871–2006 HadISST dataset and (right) the same quantities computed using the ENSO-unrelated SST anomalies. The fraction of variance explained in (a),(c) the original dataset and (b),(d) the ENSO-unrelated dataset is indicated over each panel. Note that the PCs are normalized to have unit amplitude, while the EOFs show the observed magnitude (°C) for a unit deviation of the PC. The contour interval is 0.05°C.